

Joint constraints on
reionization with the
21cm signal and kSZ

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Princeton University

Observing the
low-frequency sky
with ALBATROS



THE 21 CM SIGNAL

WHAT IS IT?

THE 21 CM SIGNAL

WHAT IS IT?

WHY DO WE CARE?

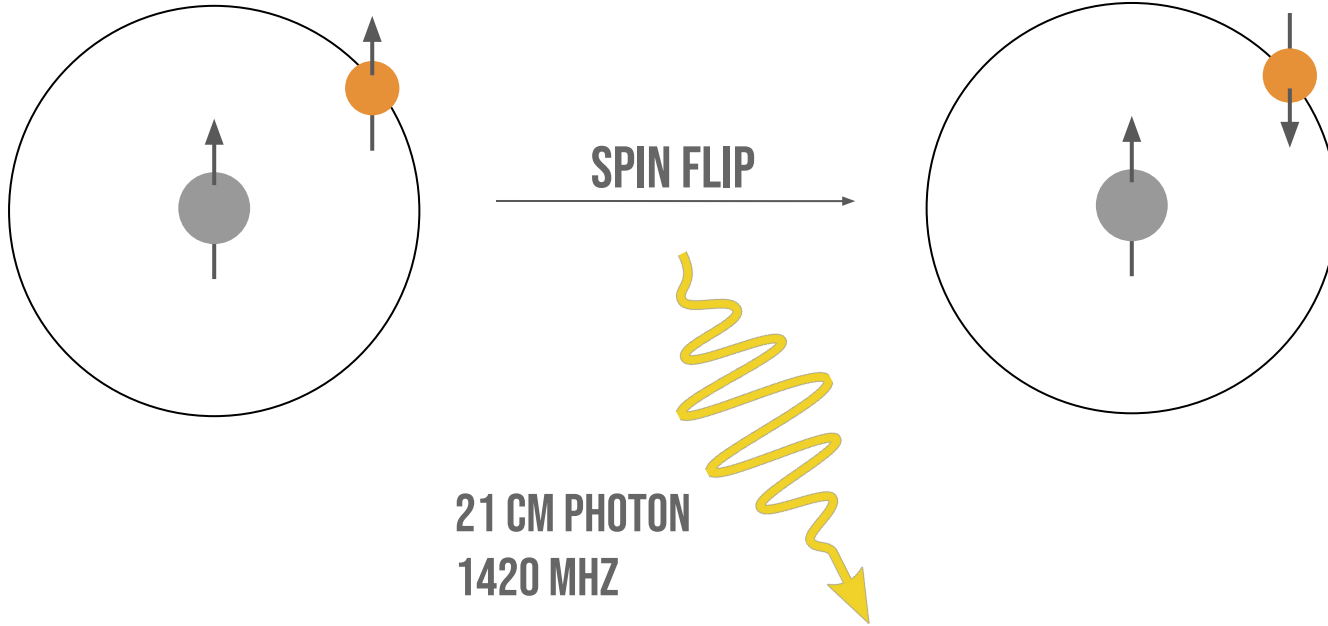
THE 21 CM SIGNAL

WHAT IS IT?

WHY DO WE CARE?

WHAT DO WE KNOW?

The 21 cm signal: What is it?



The 21 cm signal: What is it?

21cm differential
brightness temperature

$$\boxed{\delta T_b} \propto x_{\text{HI}} \frac{T_s - T_\gamma}{T_s} (1 + \delta_b)$$

The 21 cm signal: What is it?

$$\boxed{\delta T_b} \propto \boxed{x_{\text{HI}}} \frac{\boxed{T_s} - \boxed{T_\gamma}}{T_s} \left(1 + \boxed{\delta_b} \right)$$

21cm differential
brightness temperature

21 cm spin
temperature

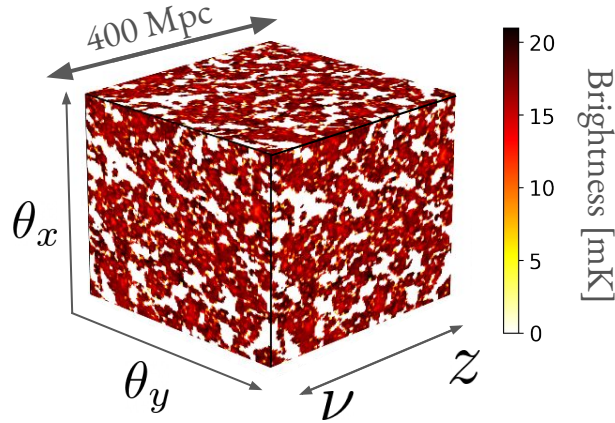
CMB temperature

Fraction of
neutral hydrogen

Baryon density

The 21 cm signal: What is it?

Mapping
fluctuations



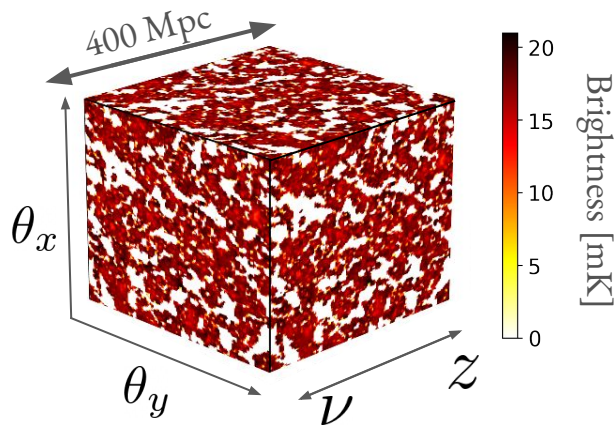
$$z = \frac{\nu_{\text{rest}}}{\nu_{\text{obs}}} - 1$$

HERA interferometer

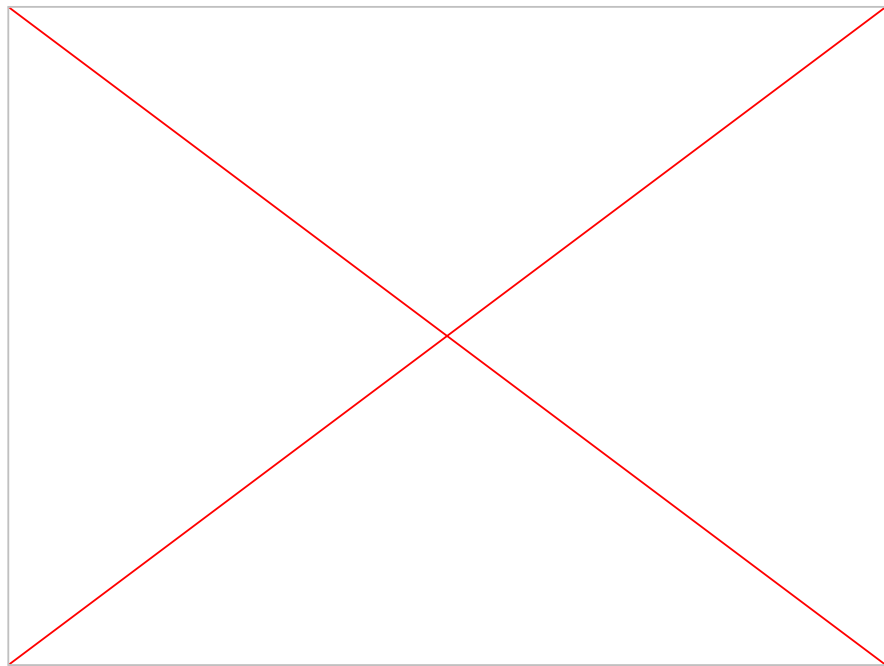


The 21 cm signal: What is it?

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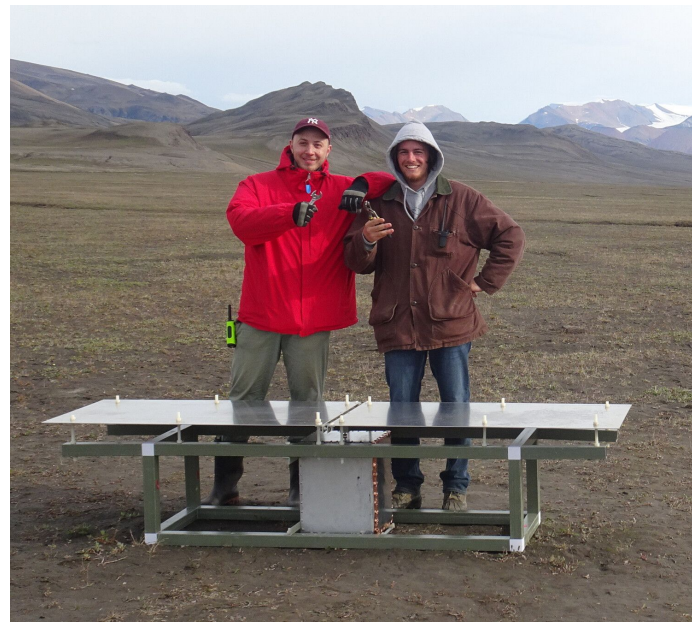
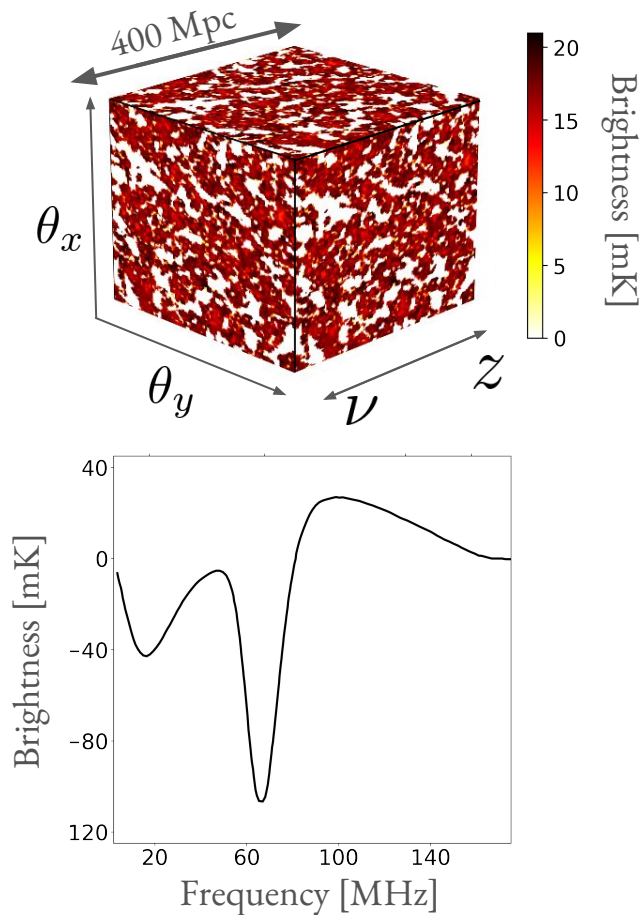


The 21 cm signal: What is it?

Mapping
fluctuations

Spatial average
↓

“Global
signal”



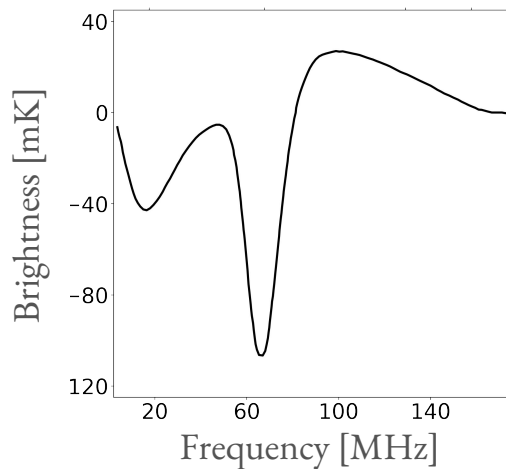
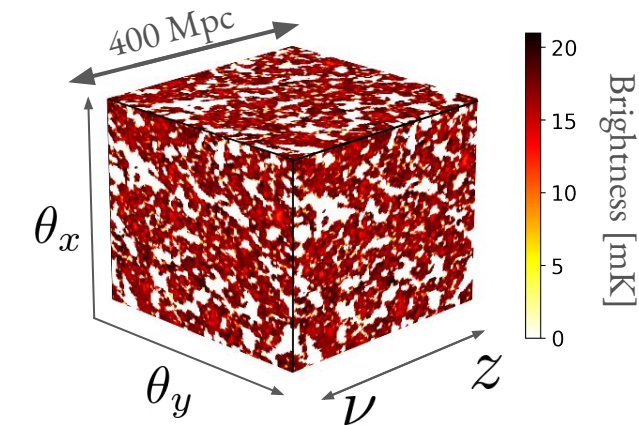
Ian Hendricksen and Vadym Vidulla at the McGill Arctic Research Station with the MIST global signal experiment

The 21 cm signal: What is it?

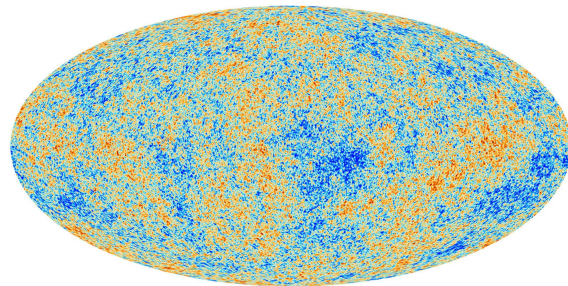
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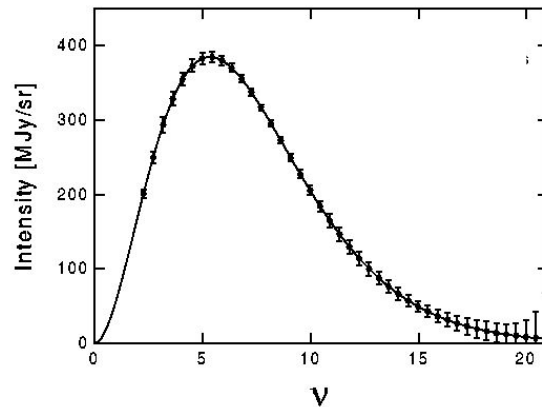
“Global
signal”



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The 21 cm signal: What can we learn?

- Gives access to large volumes of the universe: tracer of LSS in 3D.

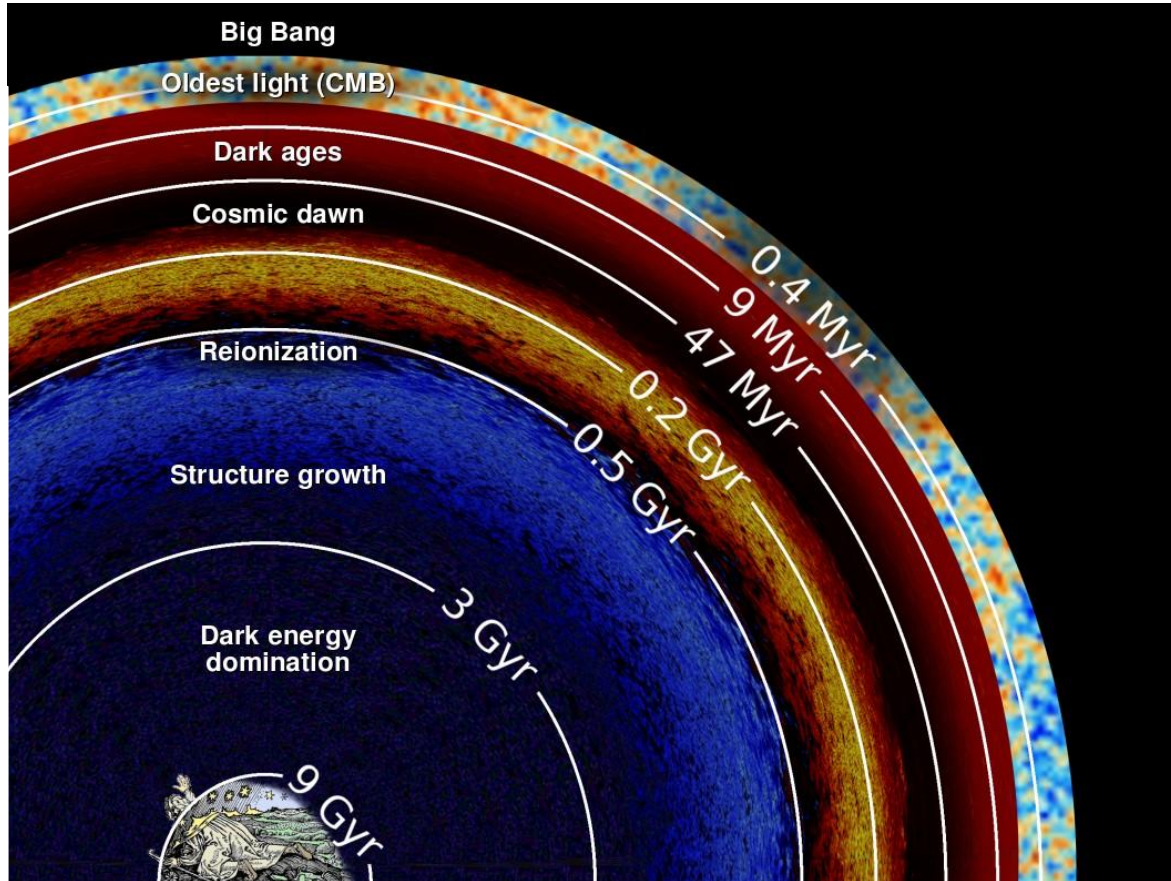


Image credits: Cynthia Chiang

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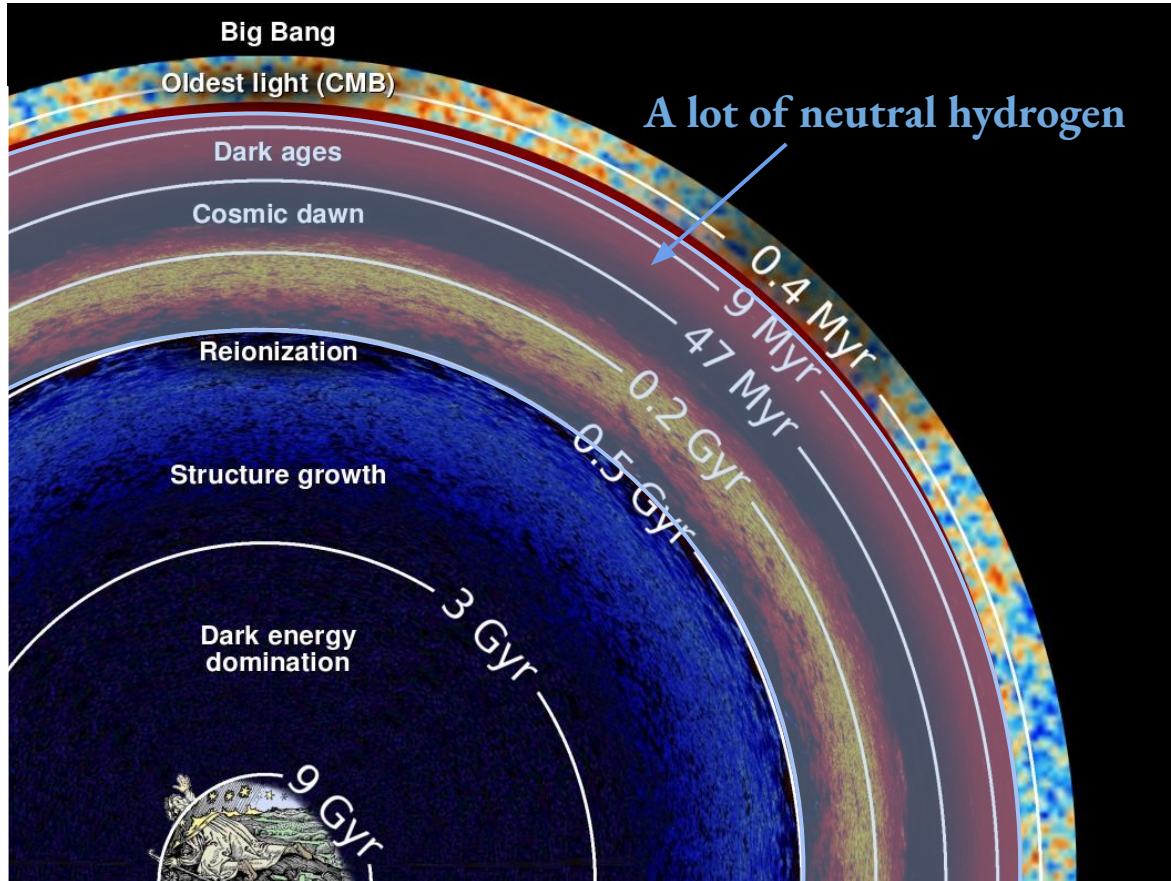
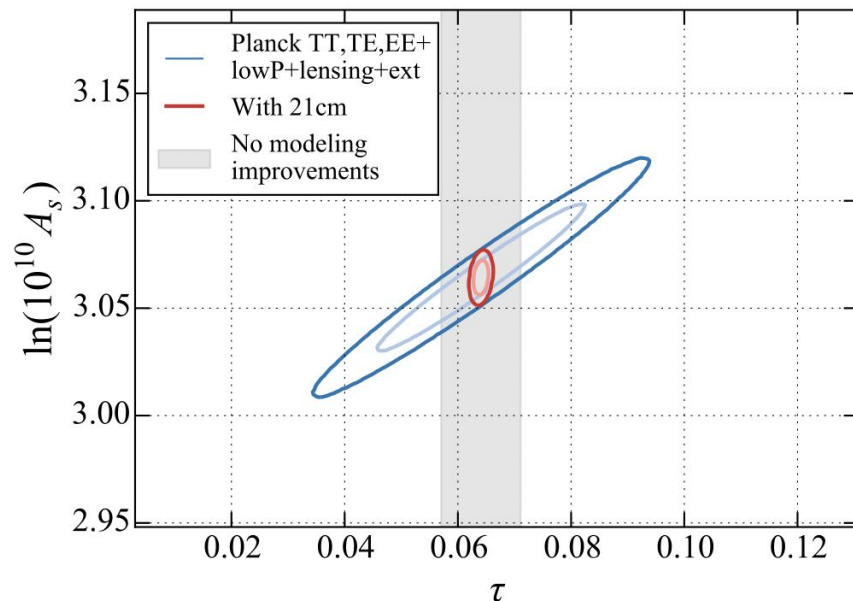
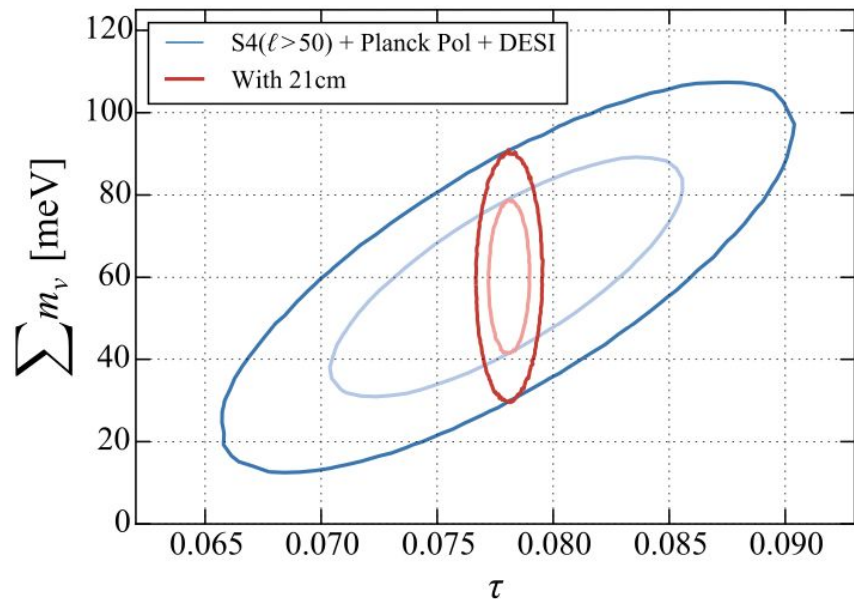


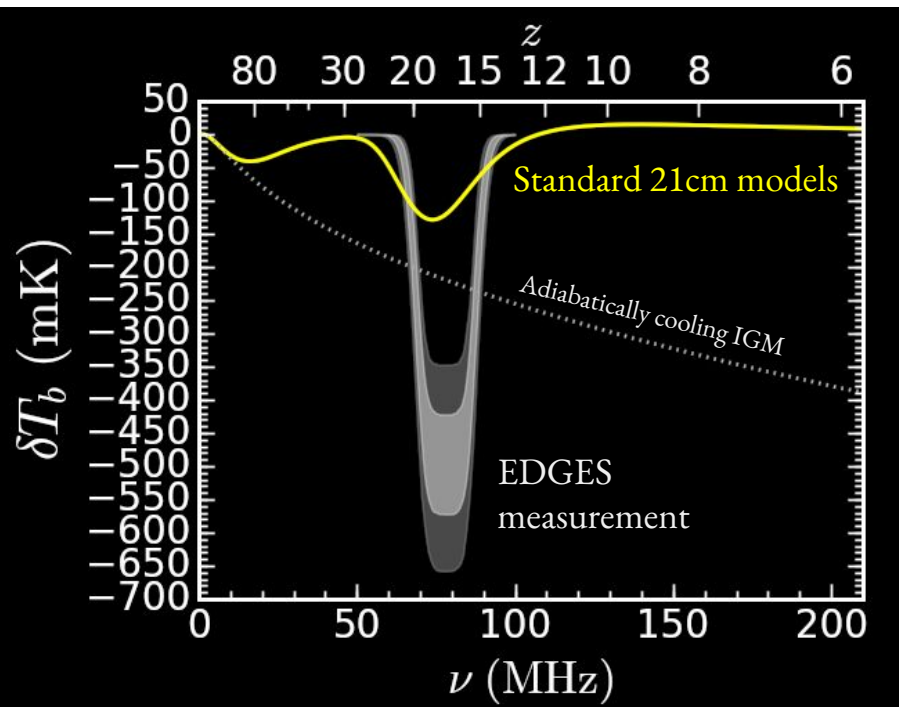
Image credits: Cynthia Chiang

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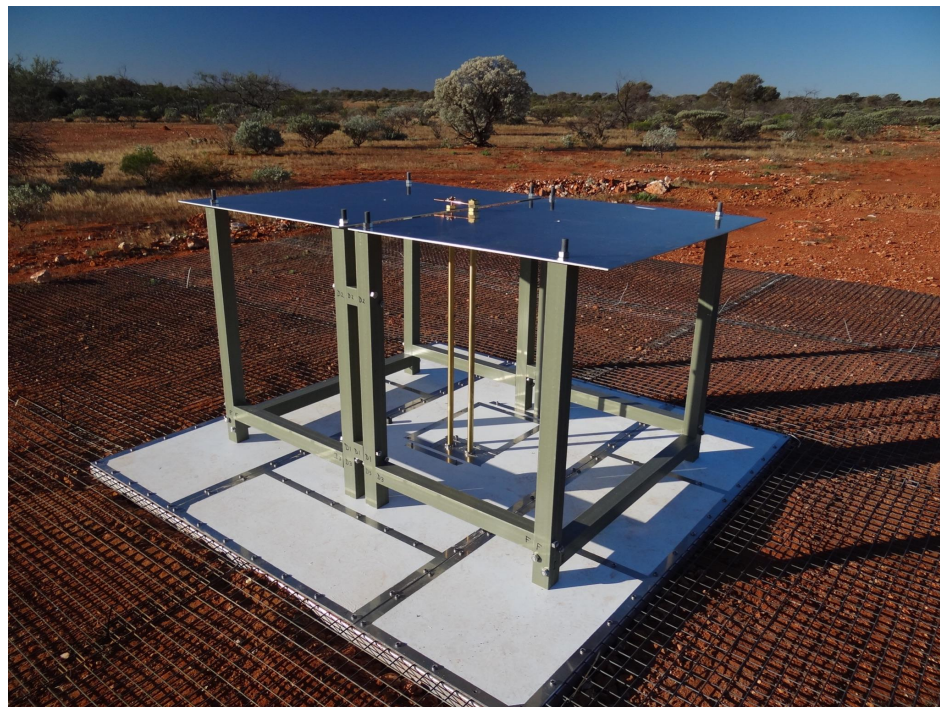
- Gives access to large volumes of the universe: tracer of LSS in 3D.
- Improved constraints on the astrophysics of the early universe.
- Potential to break degeneracies in cosmological parameters.



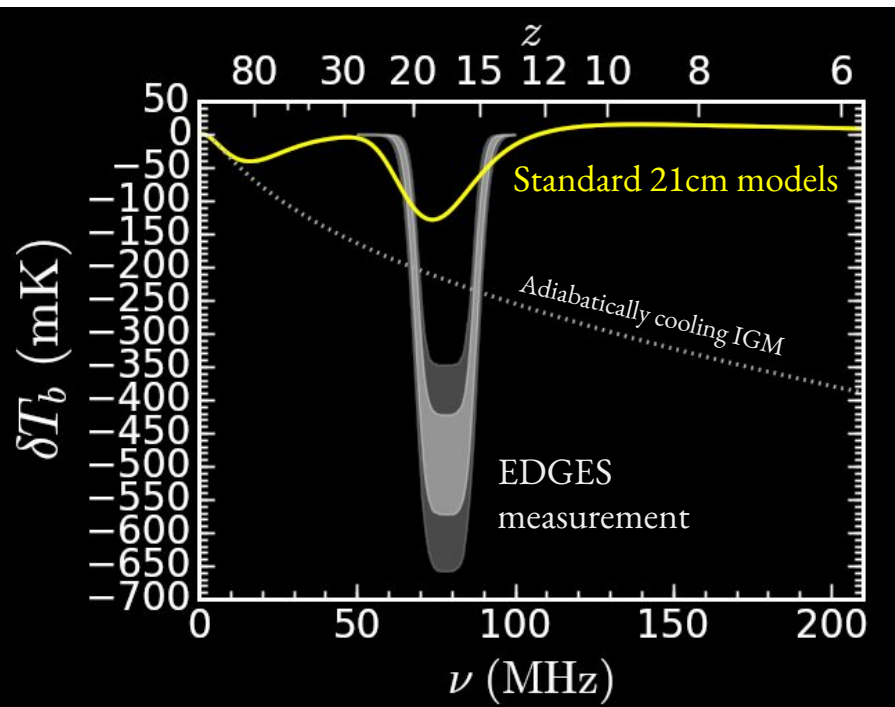
The (global) 21 cm signal: What do we know?



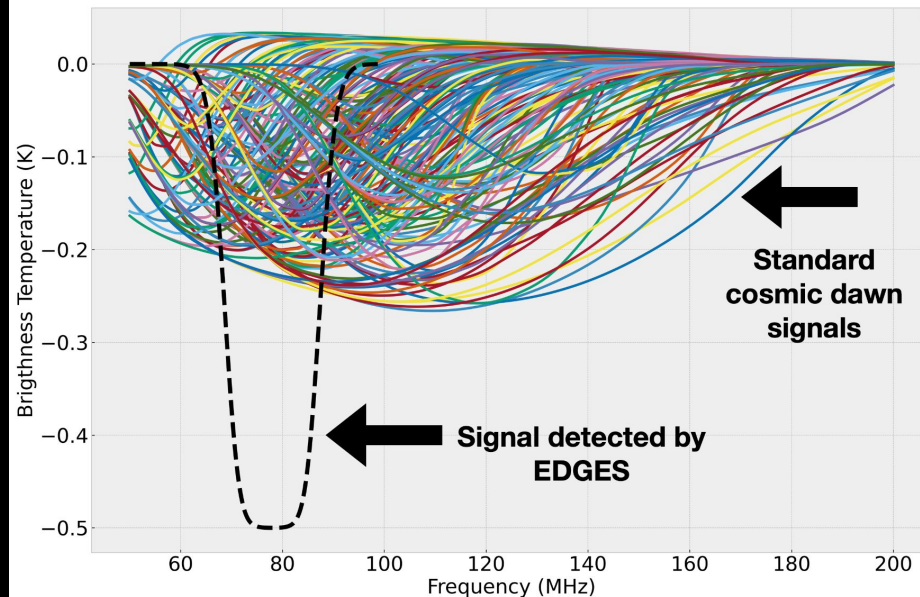
EDGES result (Bowman et al 2018)



The (global) 21 cm signal: What do we know?



EDGES result (Bowman et al 2018)



Saurabh Singh (2022)

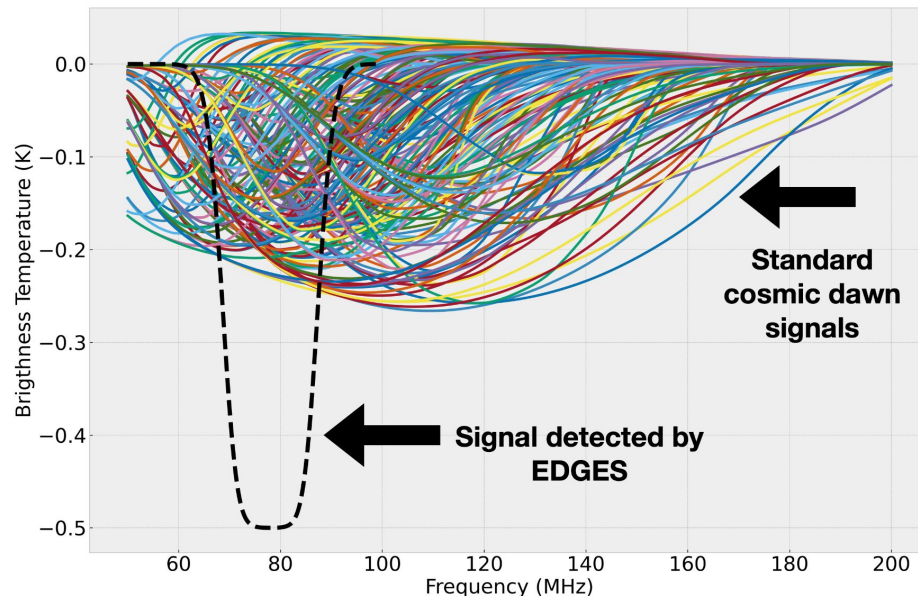
The (global) 21 cm signal: What do we know?

Exotic baryon-DM interactions, DM decay?
(1803.06698, 1802.10577, 1802.10094)

Synchrotron radiation from black holes?
(1803.01815)

Unpredicted high z radio excess?
(1802.07432)

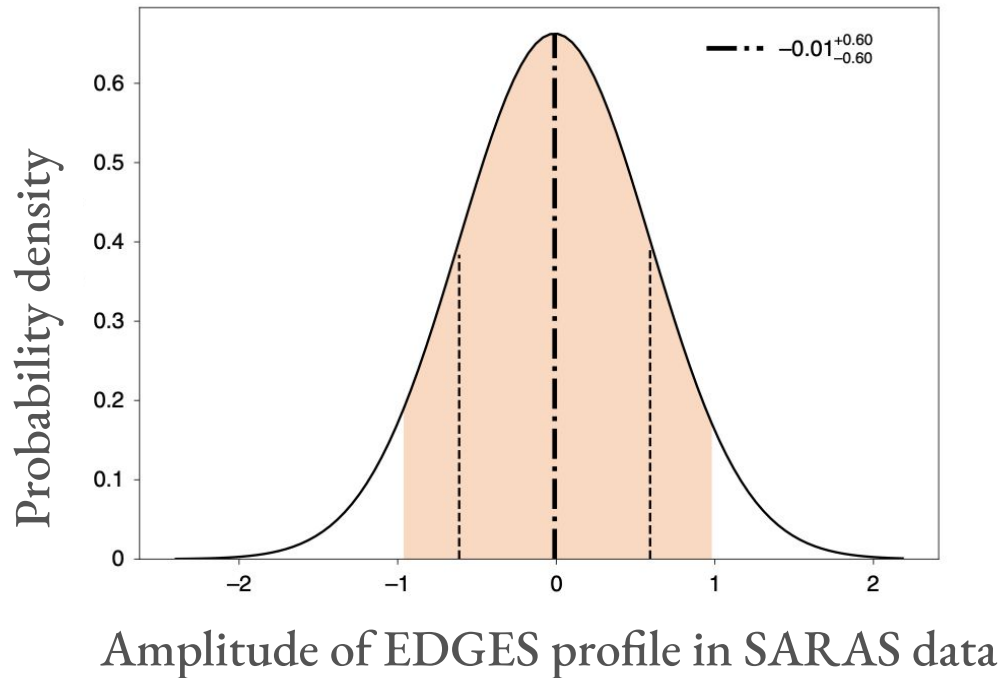
Systematics



Saurabh Singh (2022)

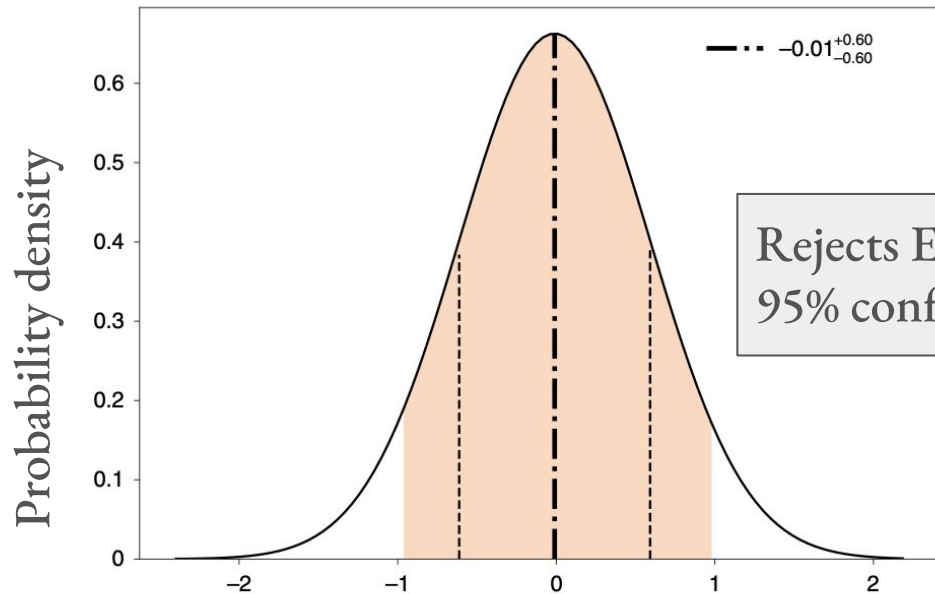
The (global) 21 cm signal: What do we know?

SARAS experiment: follow up to EDGES



The (global) 21 cm signal: What do we know?

SARAS experiment: follow up to EDGES



Rejects EDGES profile at 95% confidence.

Amplitude of EDGES profile in SARAS data



WHAT IS THE 21 CM SIGNAL?

Redshifted emission from neutral hydrogen's hyperfine transition.

WHAT CAN WE LEARN FROM IT?

Evolution of large scale structure for $z > 6$.

Early universe astrophysics.

Potentially break degeneracies in cosmological parameters.

WHAT DO WE KNOW?

One detection of the global signal at 80 MHz + follow up
non-detection.

Constraining reionization with the global 21cm signal and kSZ

In collaboration with Adrian
Liu and Adelie Gorce

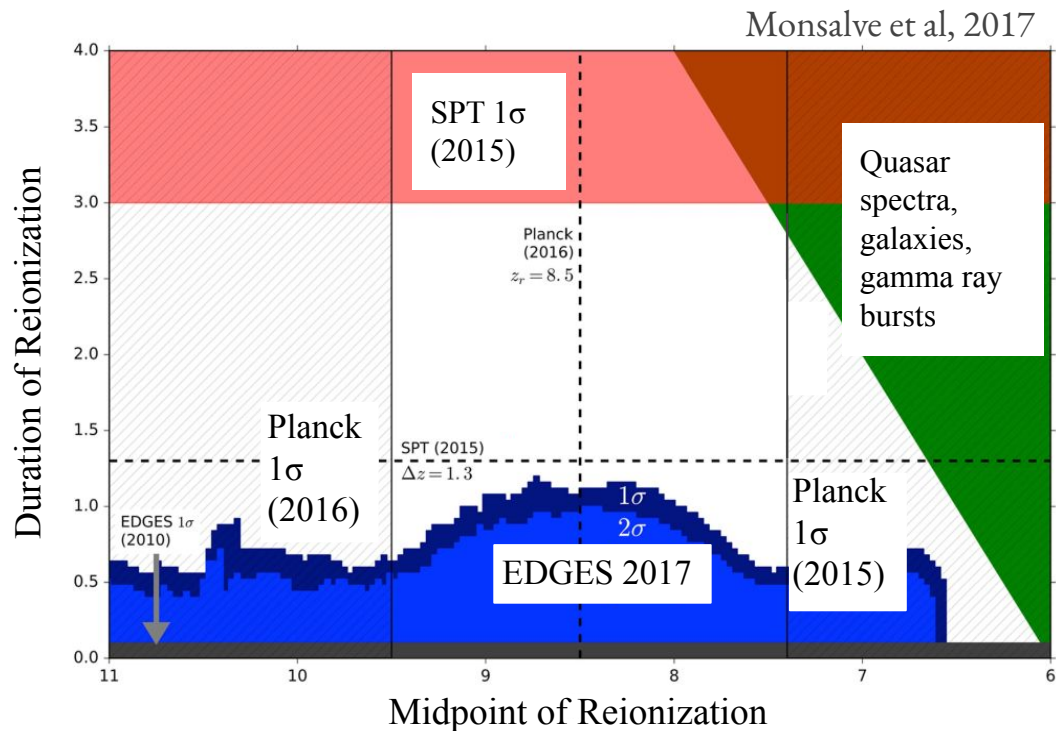
The ionization history

$$\tau \propto \int dz \, x_{\text{HII}}(z)$$

Fraction of ionized hydrogen

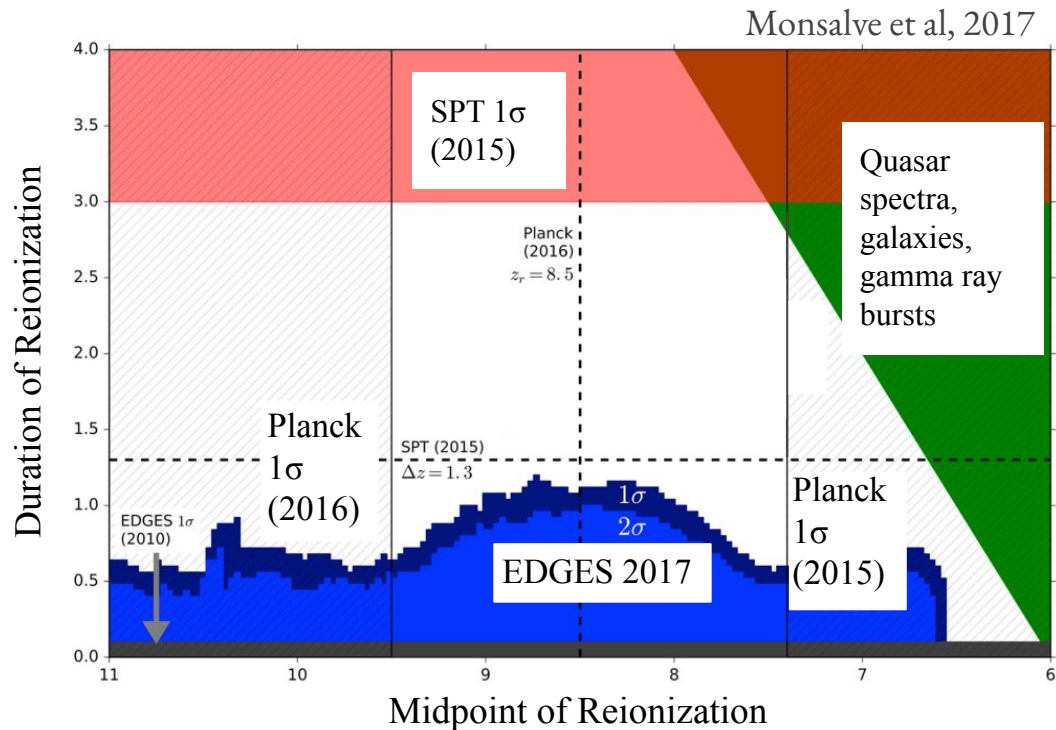
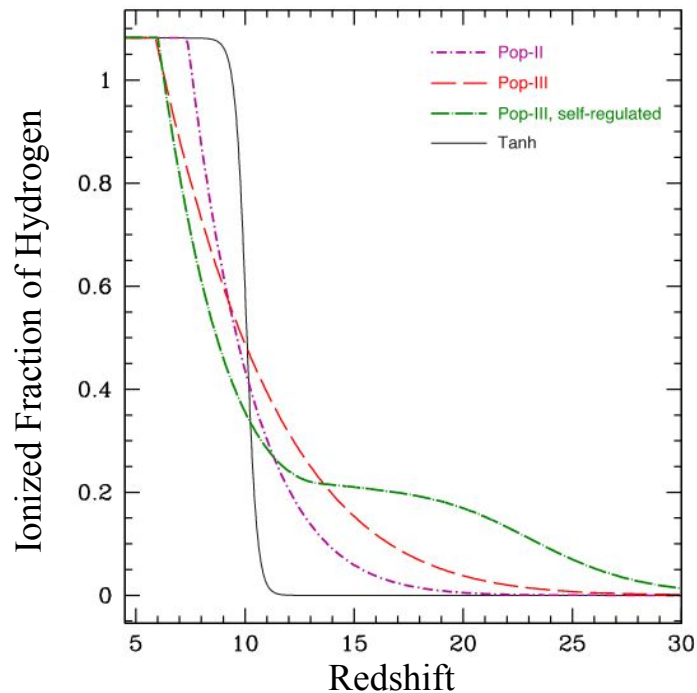
The ionization history

- Some bounds on midpoint, end, and duration.



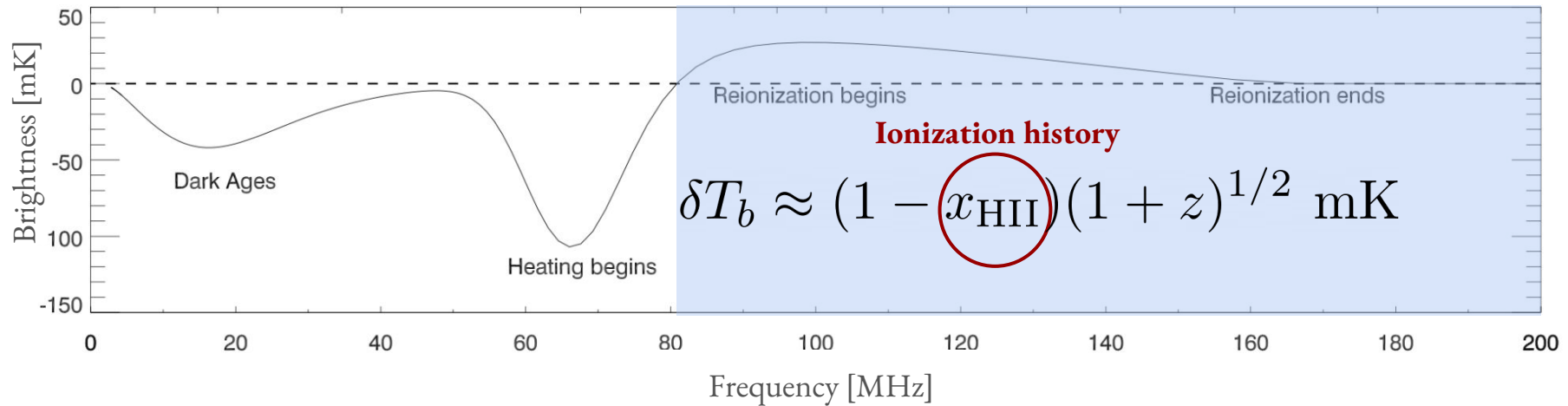
The ionization history

- Some bounds on midpoint, end, and duration.
- Few limits on precise shape.



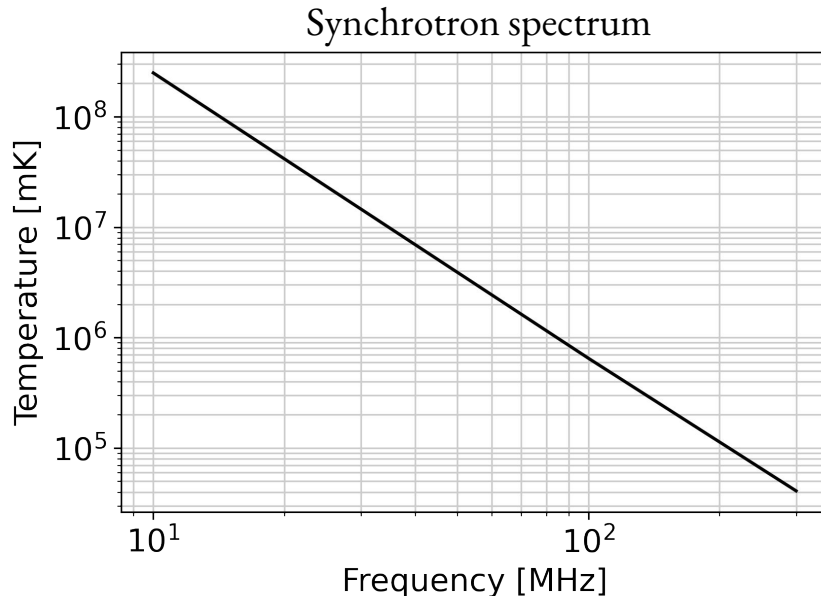
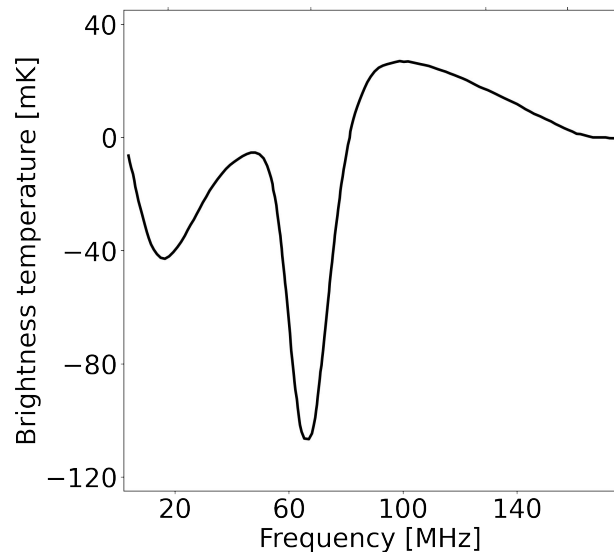
The global 21cm signal as a probe of reionization

- During reionization, the global signal closely tracks the ionization history



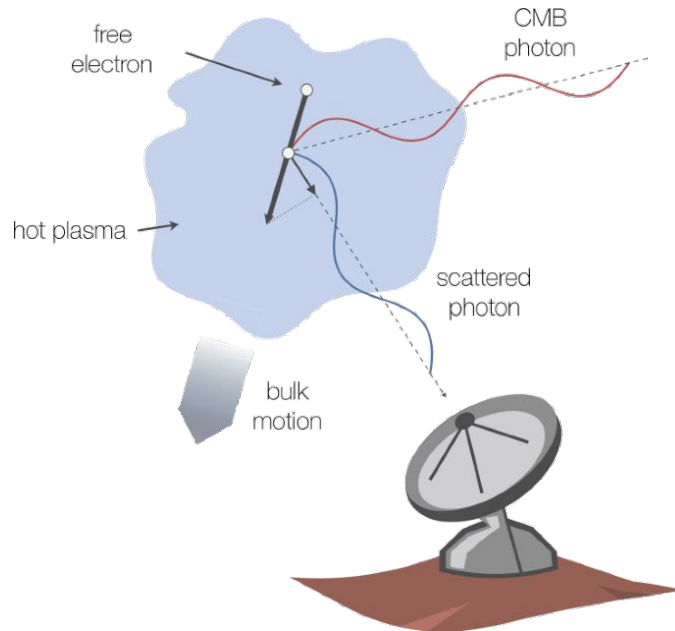
The global 21cm signal as a probe of reionization

- During reionization, the global signal closely tracks the ionization history
- The global signal is **most sensitive to rapidly evolving reionization histories** due to spectrally smooth foregrounds



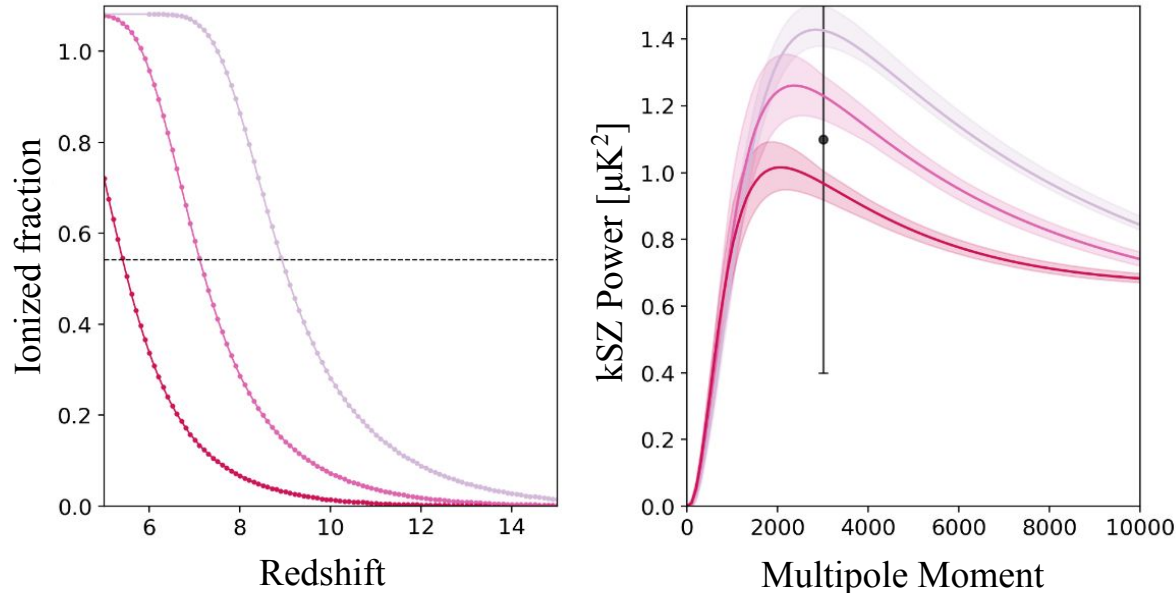
The kinetic Sunyaev-Zeldovich effect (kSZ)

- CMB photons scattering off of energetic electrons with bulk relative velocity
- Power spectrum changes with midpoint, duration, morphology of reionization



The kinetic Sunyaev-Zeldovich effect (kSZ)

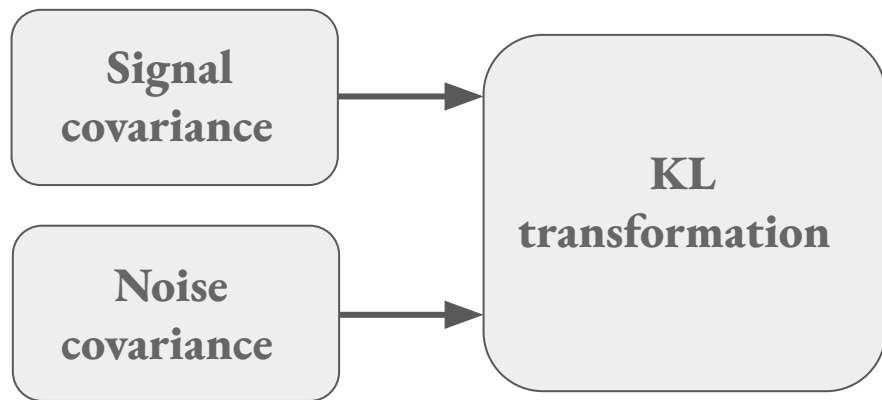
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- Power spectrum changes with midpoint, duration, morphology of reionization



The global signal is sensitive to
rapidly evolving ionization
histories, the kSZ to **extended**
ionization histories.

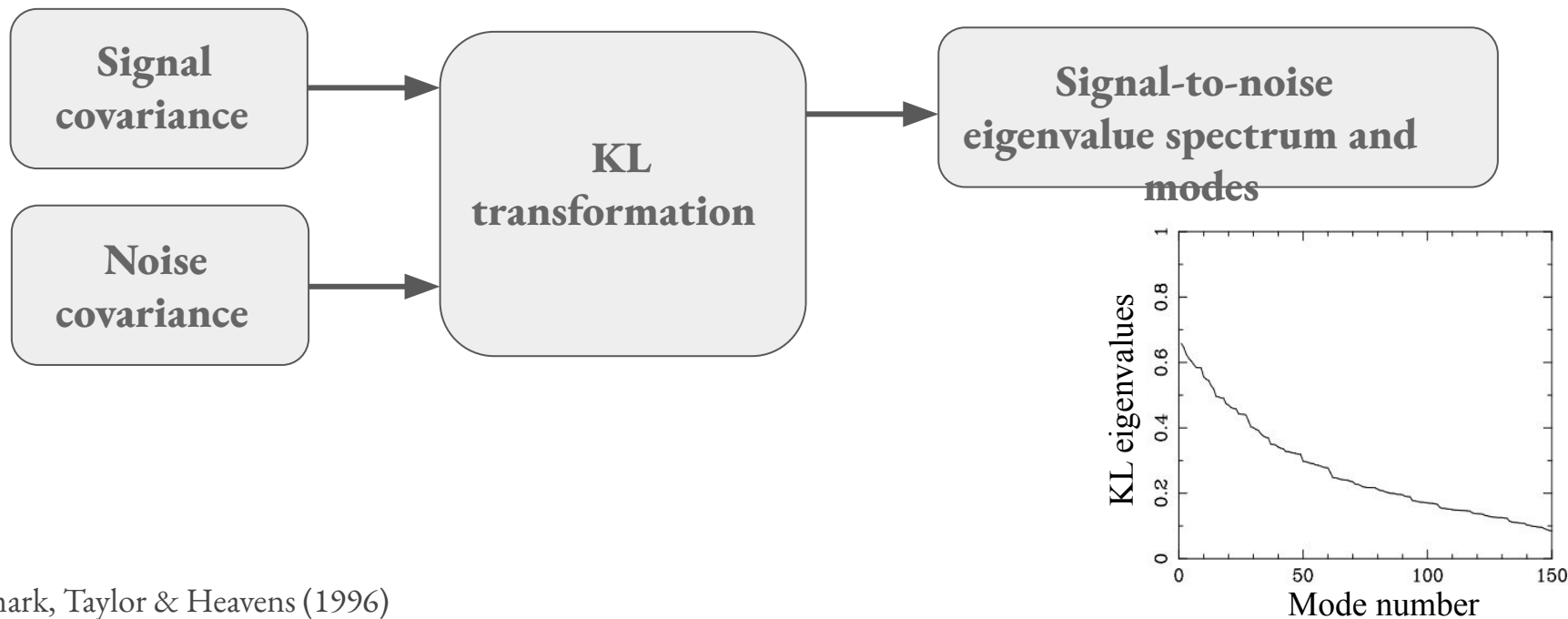
The Karhunen-Loève (KL) Transform

- A transformation whose eigenvalues represent the ratio of two signals.
- Familiar example: signal-to-noise analysis and data compression.



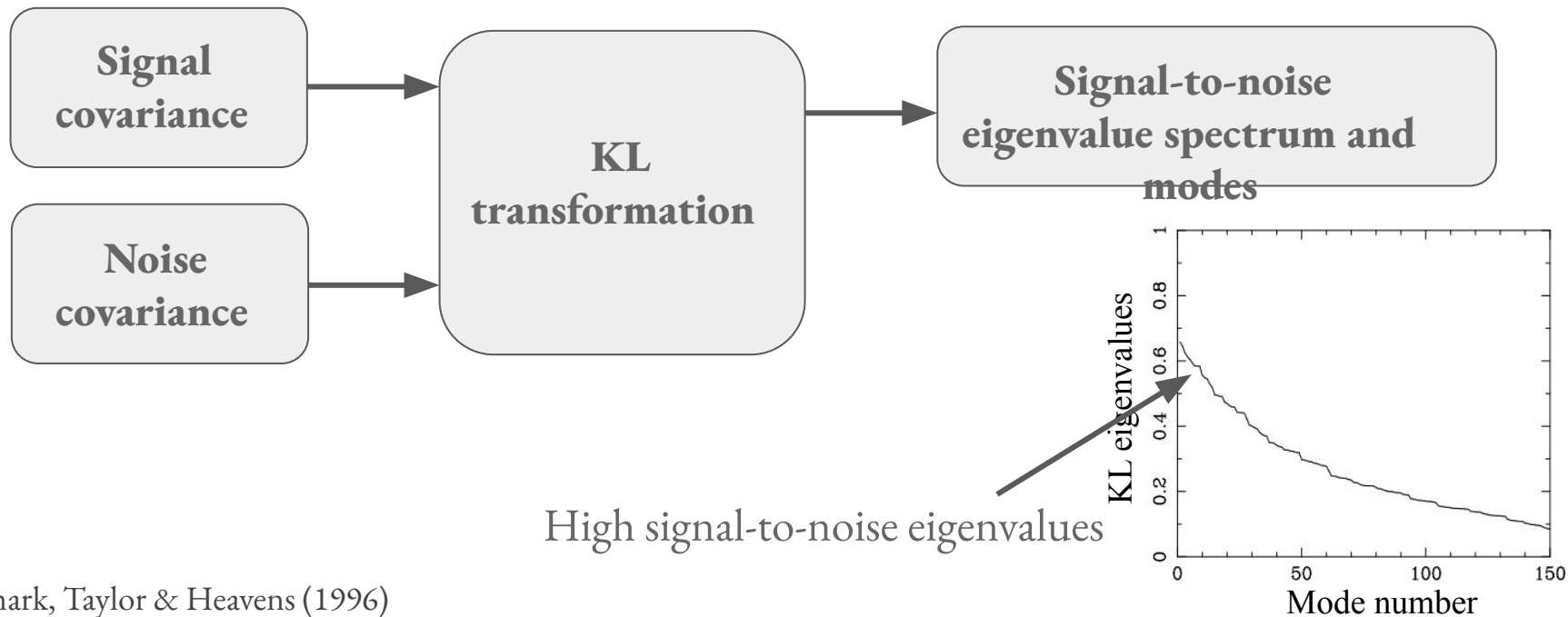
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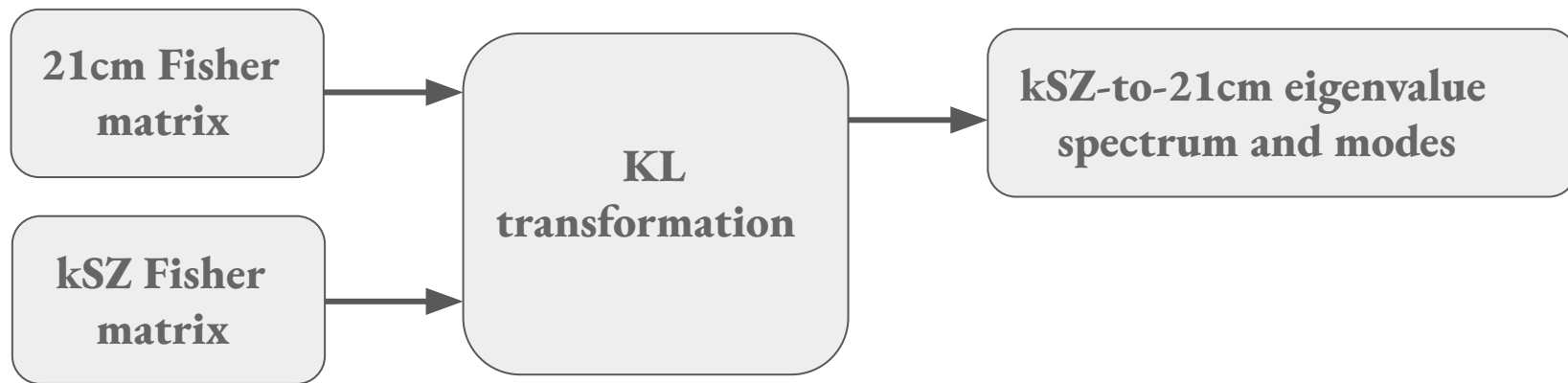
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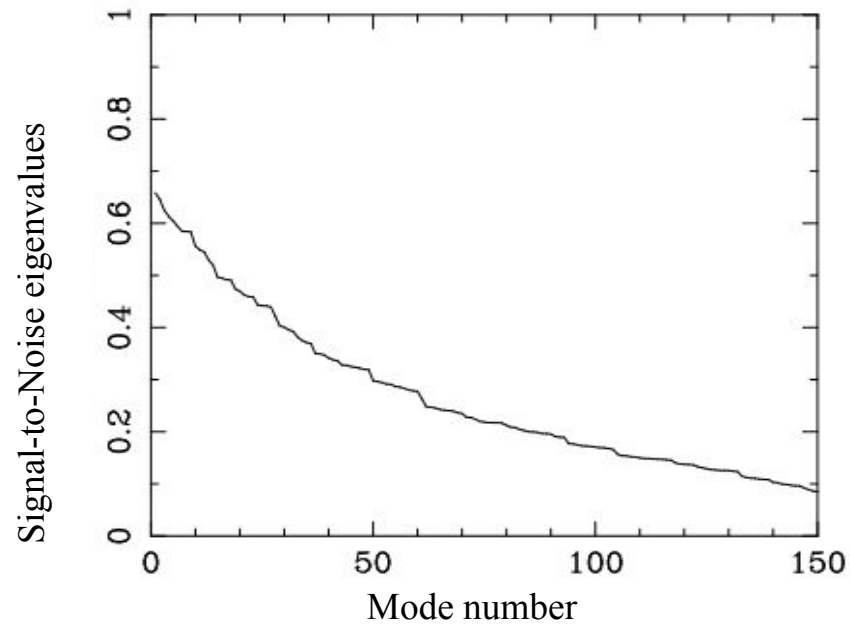
The Karhunen-Loève (KL) Transform

- In our case: kSZ-to-21cm analysis
- Fisher matrices computed with analytic 21cm and kSZ models



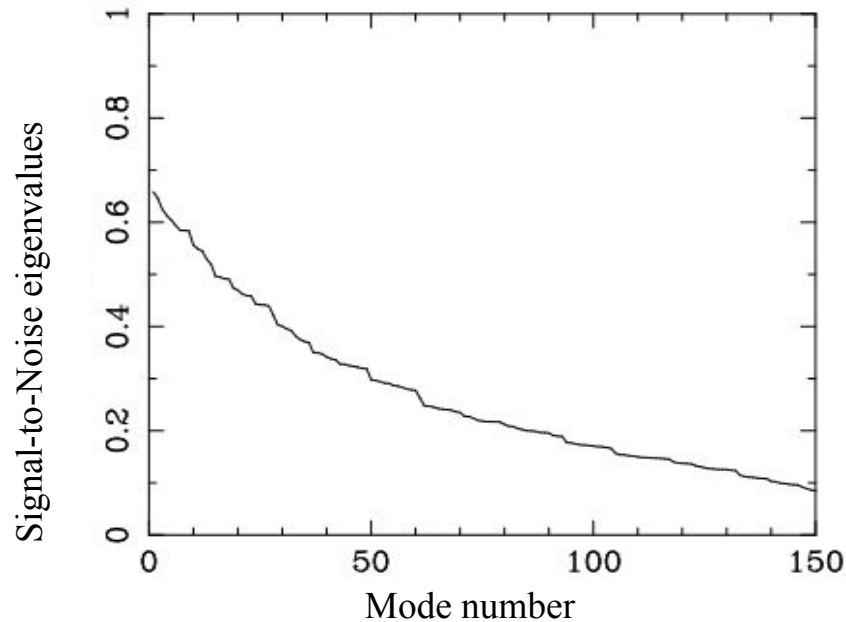
$$\mathbf{F}_{\text{kSZ}} \mathbf{v} = \lambda \mathbf{F}_{21} \mathbf{v}$$

21cm-to-kSZ eigenvalues and modes

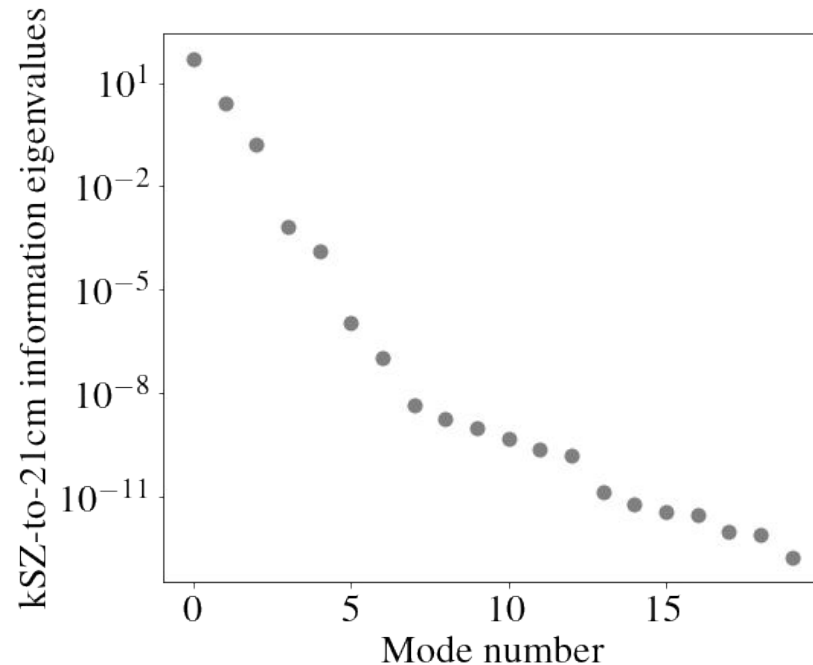


Tegmark, Taylor & Heavens (1996)

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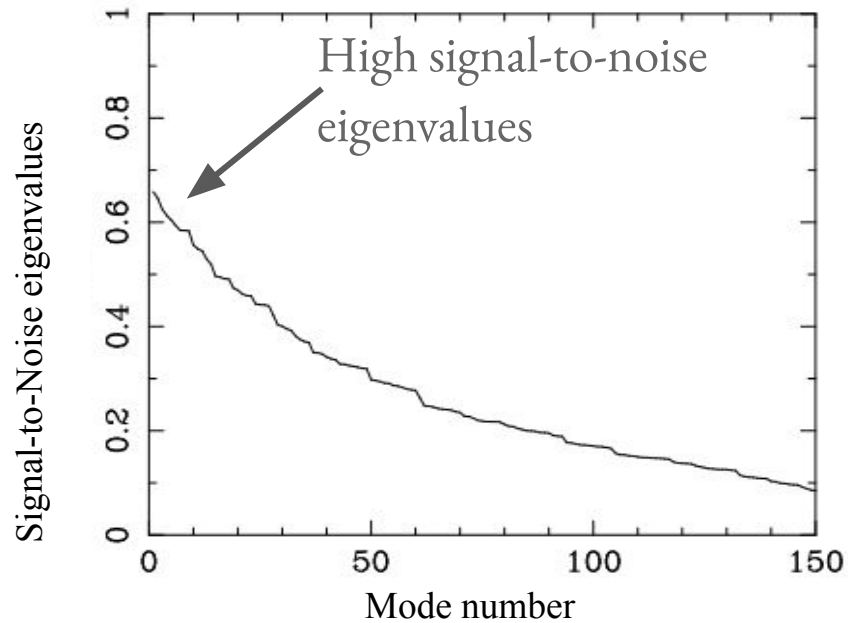


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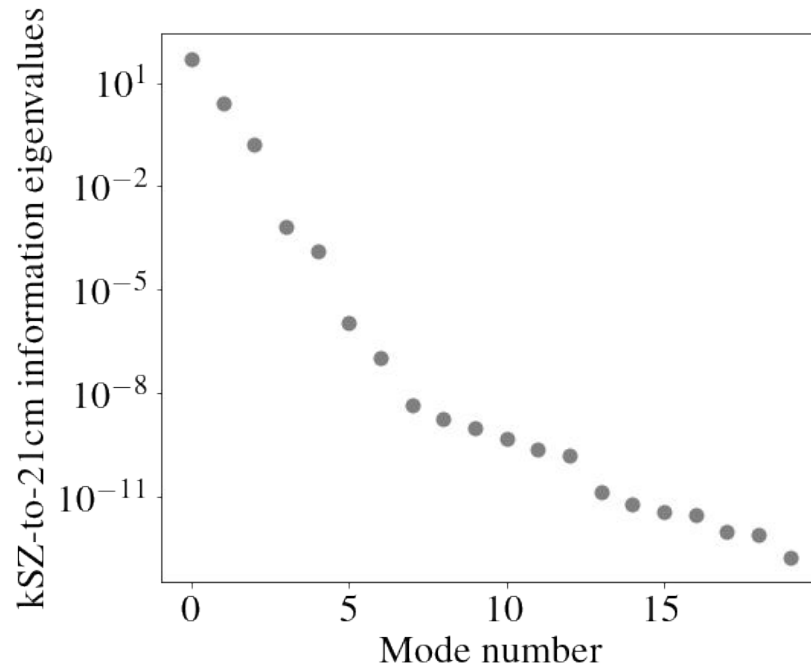


Begin, Liu & Gorce

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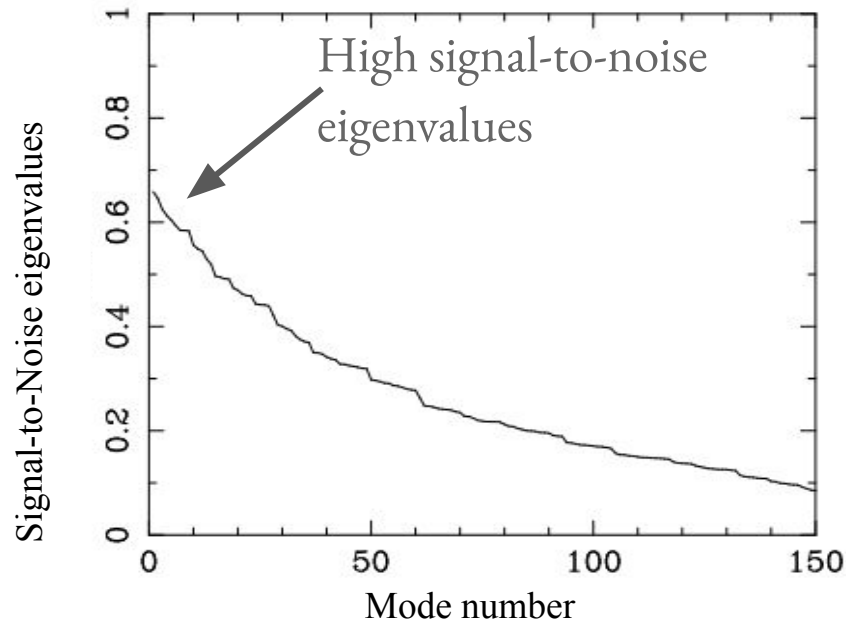


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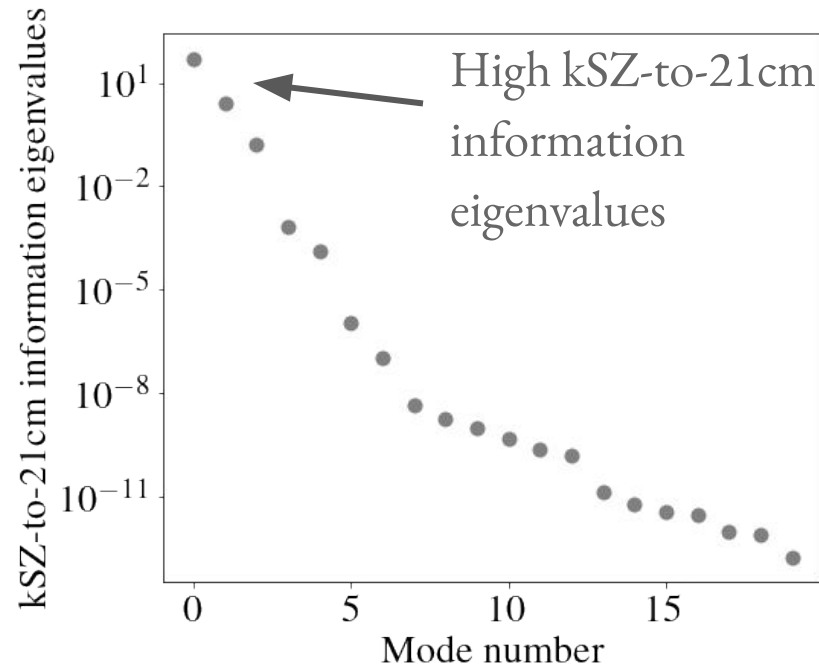


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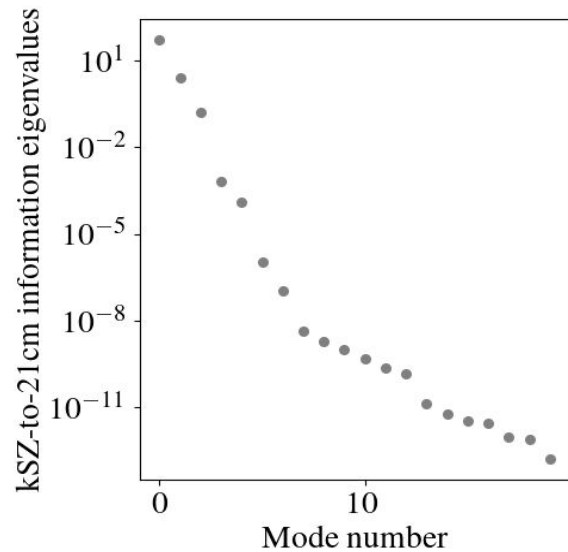


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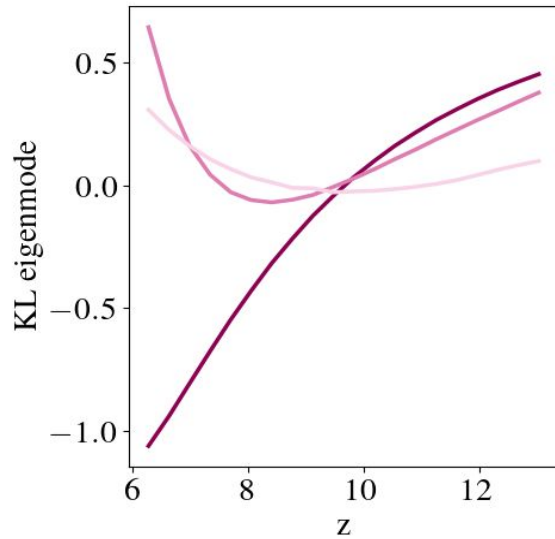
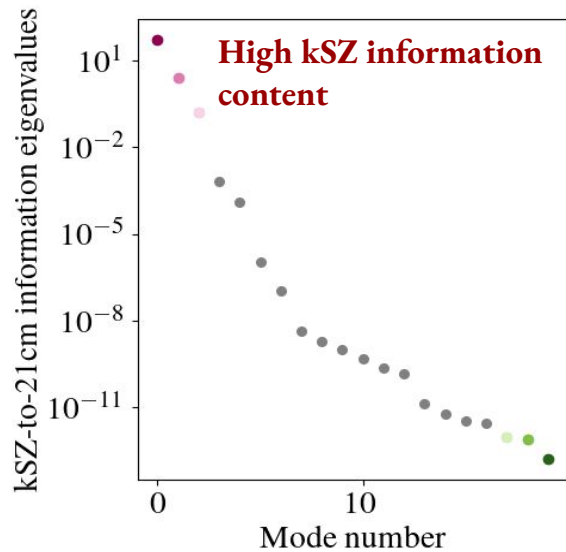


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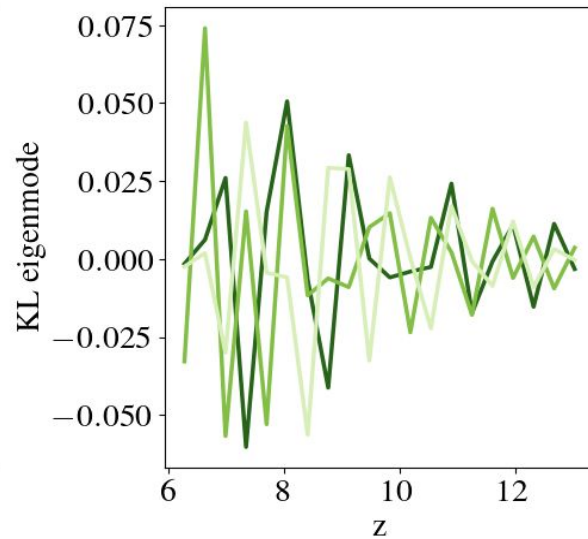
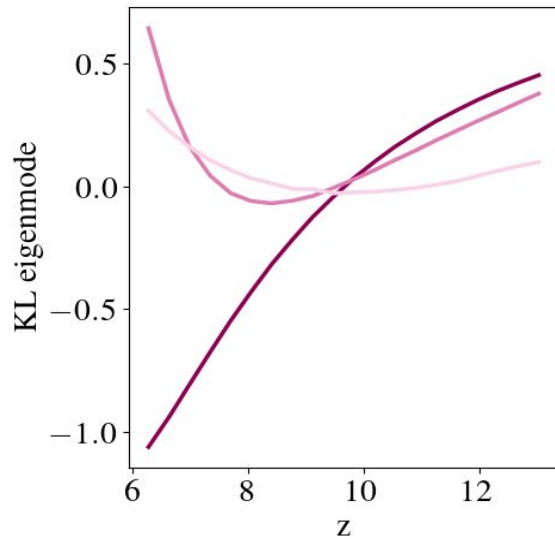
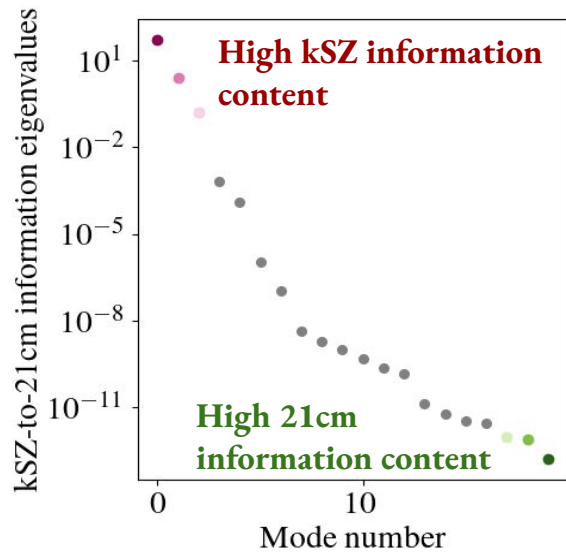
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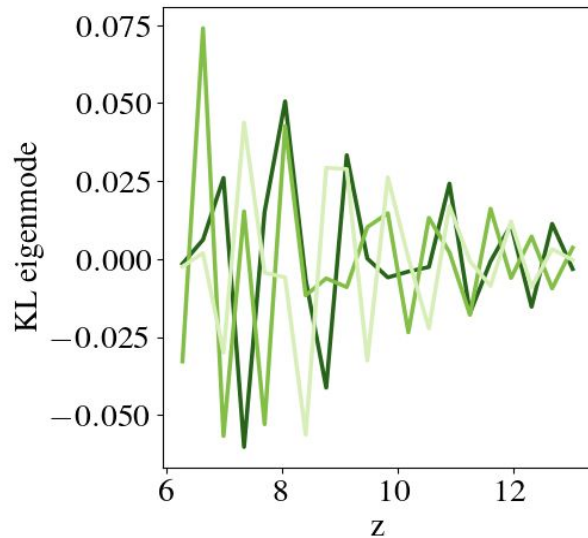
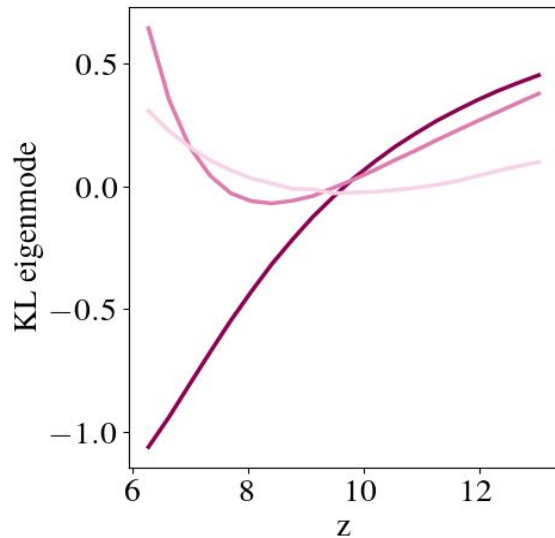
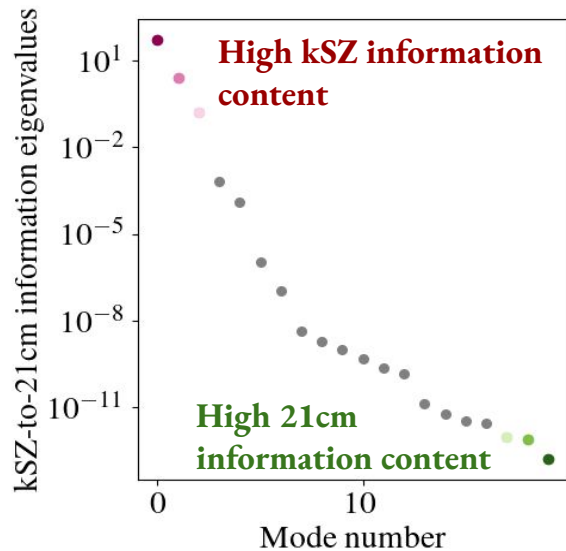
21cm-to-kSZ eigenvalues and modes



21cm-to-kSZ eigenvalues and modes



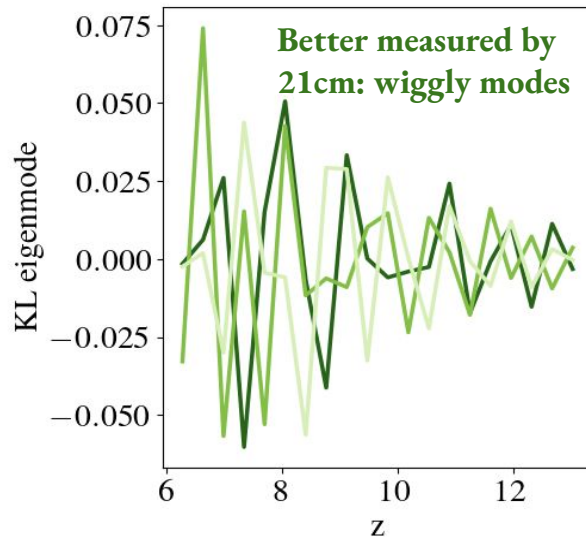
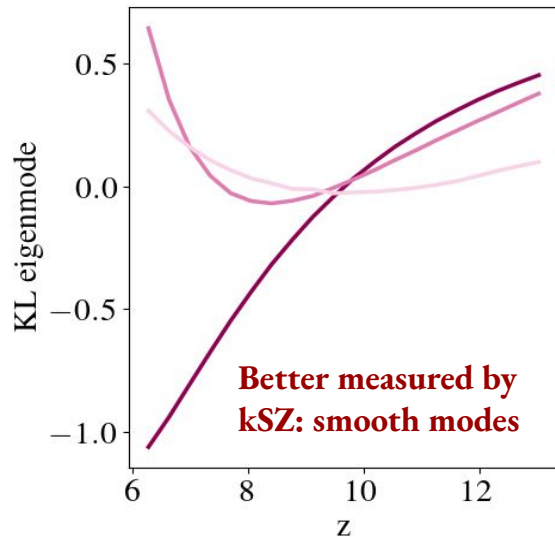
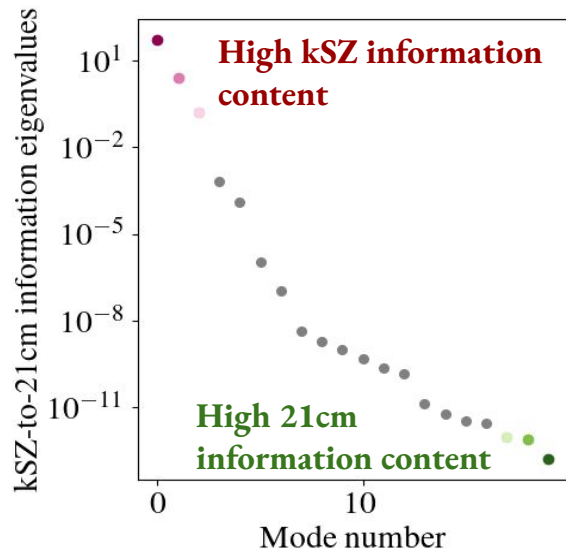
21cm-to-kSZ eigenvalues and modes



$$x_{HI}(z) = \sum_i a_i \phi_i(z)$$

KL modes

21cm-to-kSZ eigenvalues and modes



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KL modes

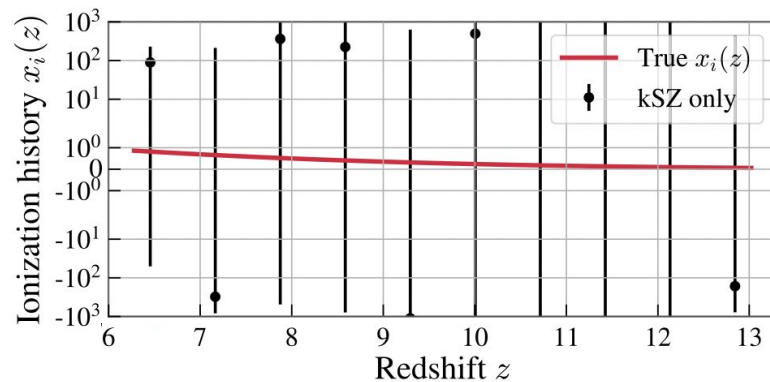
Constraining reionization: linear least squares

Measurement of KL
amplitudes by **kSZ**

$$\boxed{\mathbf{y}} = \mathbf{A} \boxed{\mathbf{x}} + \mathbf{n}$$

“True” ionization history

$$\hat{\mathbf{x}} = (\mathbf{A}^T \mathbf{N}^{-1} \mathbf{A})^{-1} \mathbf{A}^T \mathbf{N}^{-1} \mathbf{y}$$



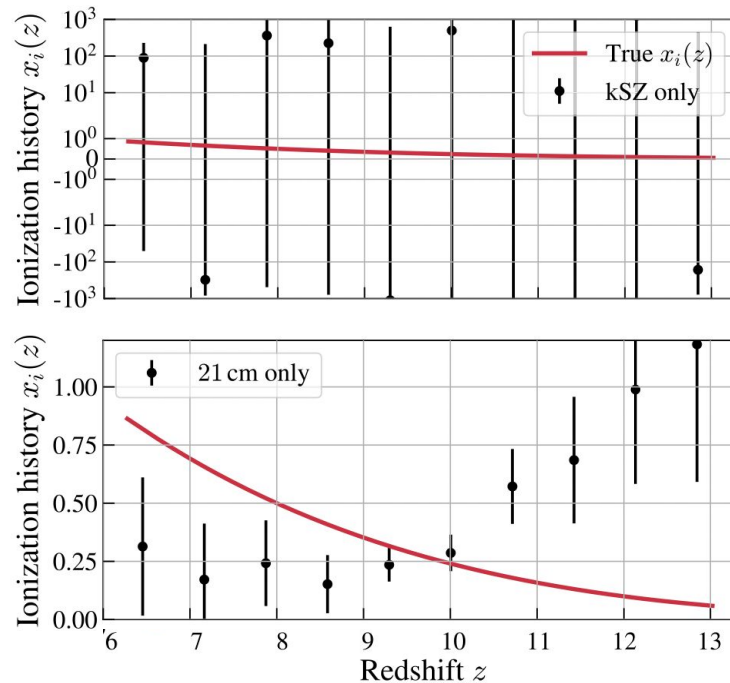
Constraining reionization: linear least squares

Measurement of KL
amplitudes by **21cm**

$$\boxed{\mathbf{y}} = \mathbf{A} \boxed{\mathbf{x}} + \mathbf{n}$$

“True” ionization history

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Constraining reionization: linear least squares

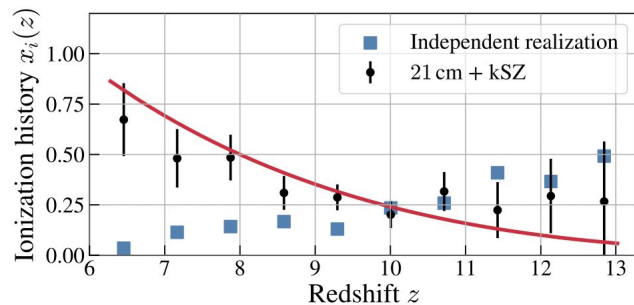
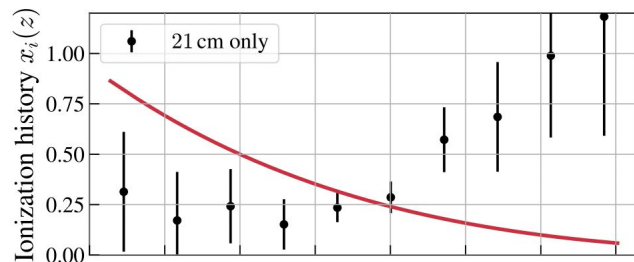
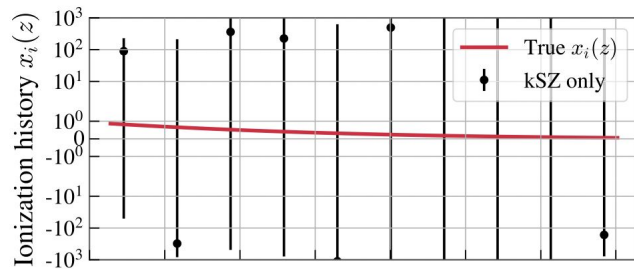
Concatenated 21cm
and kSZ measurements

$$\boxed{\mathbf{y}} = \mathbf{A} \boxed{\mathbf{x}} + \mathbf{n}$$

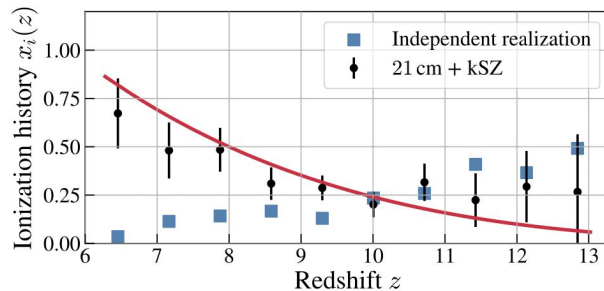
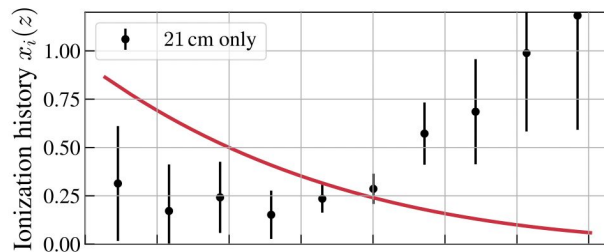
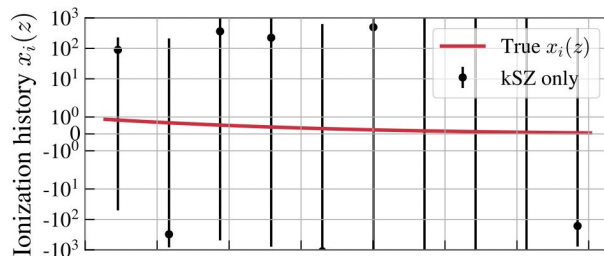
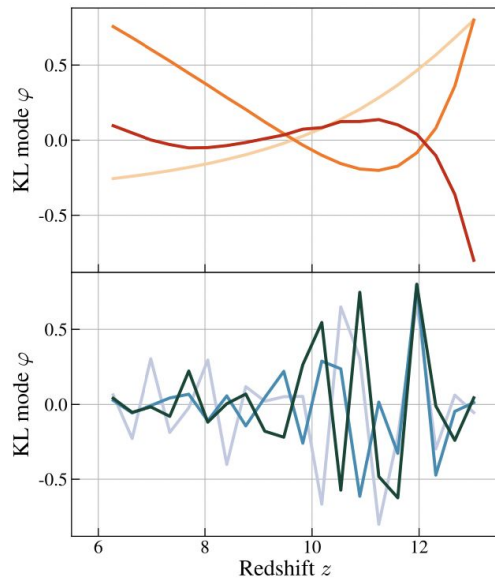
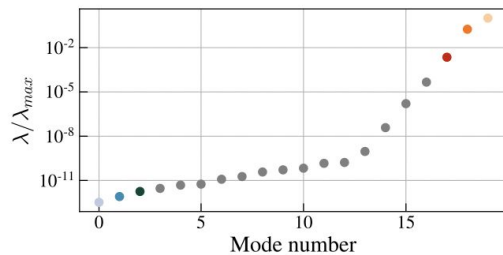
“True” ionization history

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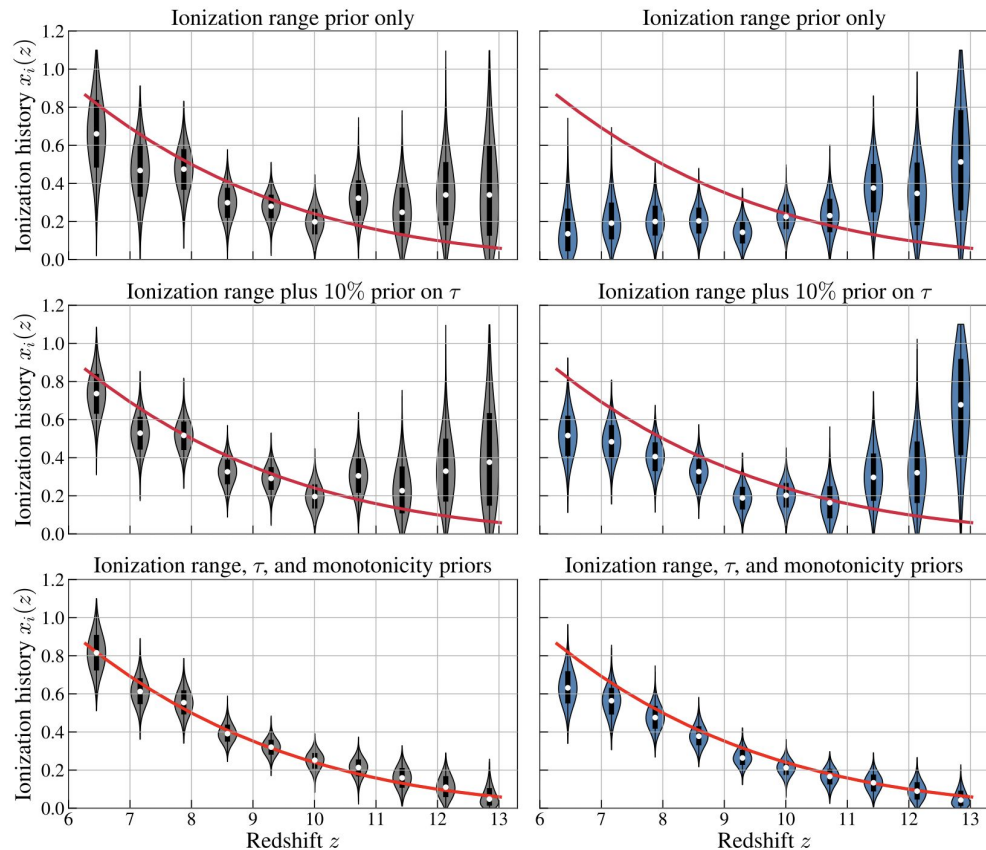
Assumes no parametrization of the ionization history.



Constraining reionization: linear least squares

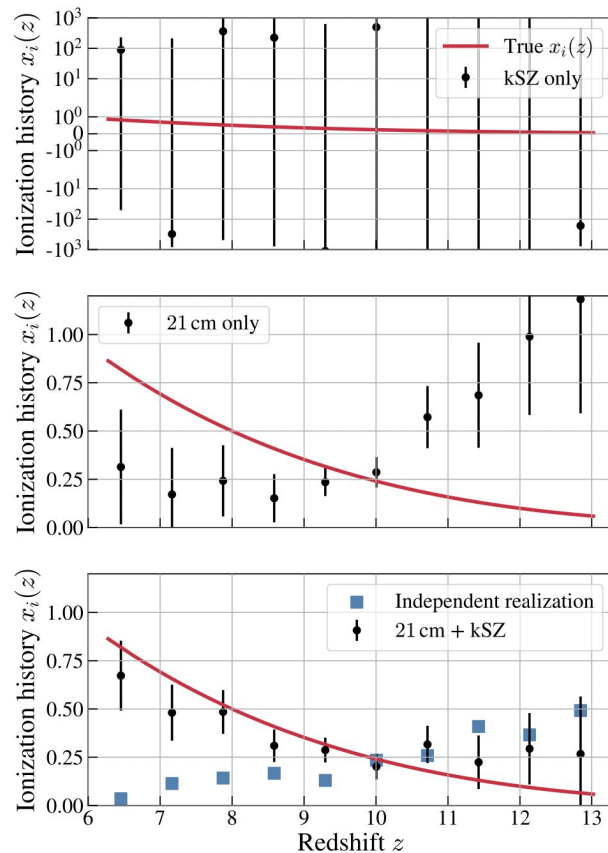


Constraining reionization: Bayesian methods

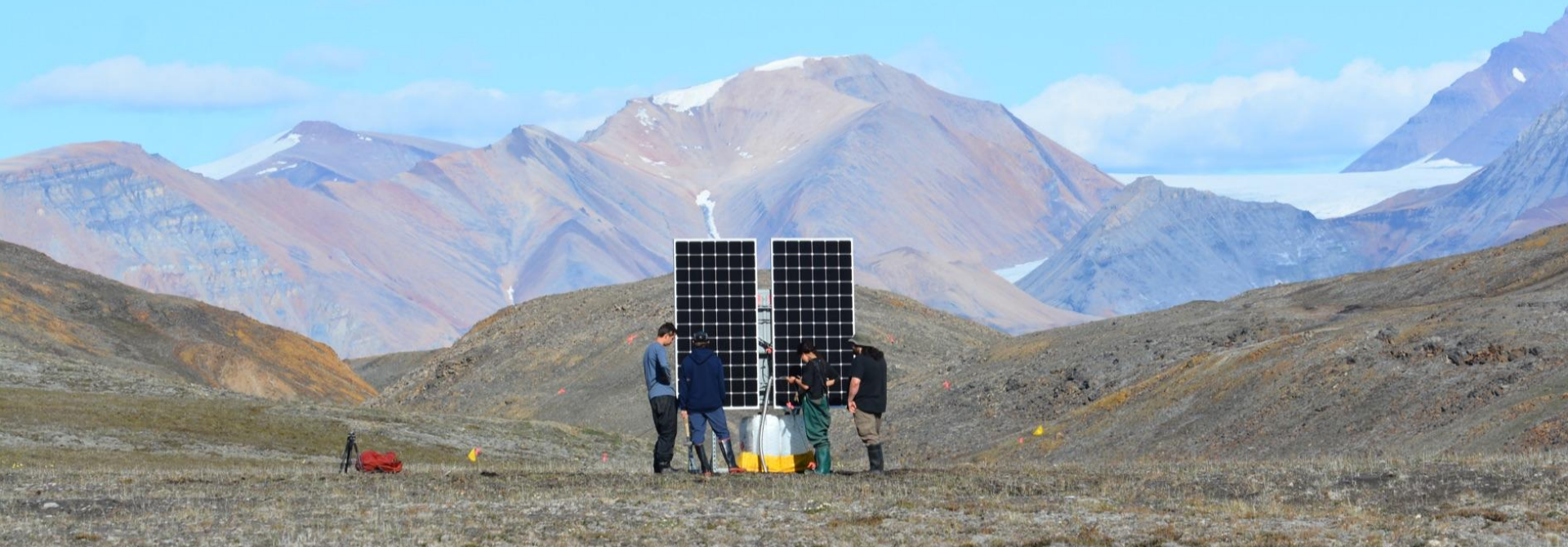


Summary

- The Karhunen-Loève basis highlights the complementary relation between the kSZ and 21cm global signal.
 - Combining these two gives us access to modes of the ionization history that each probe in isolation does not constrain.
 - KL basis facilitates detection of systematic by harnessing “overlap modes”.
- (Begin, Liu & Gorce: 2112.06933)
- This is a general framework that can be **extended to any two probes**.



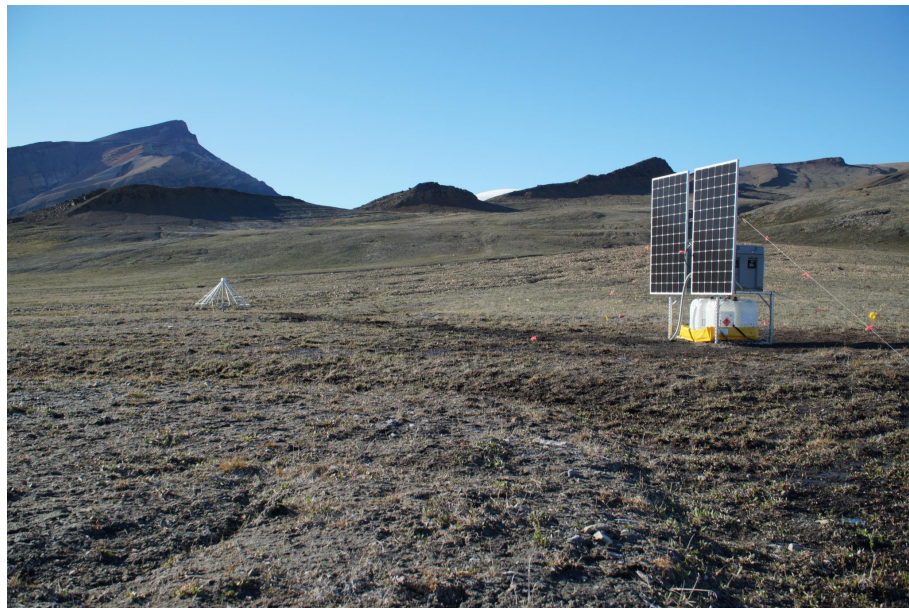
Observing the low-frequency sky with ALBATROS



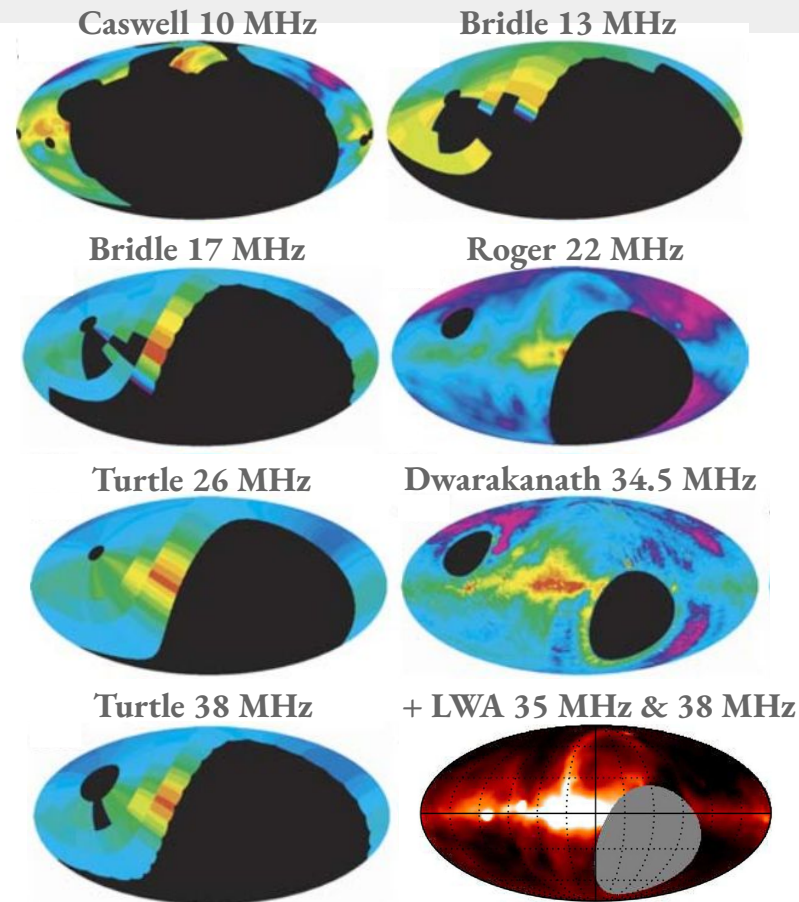
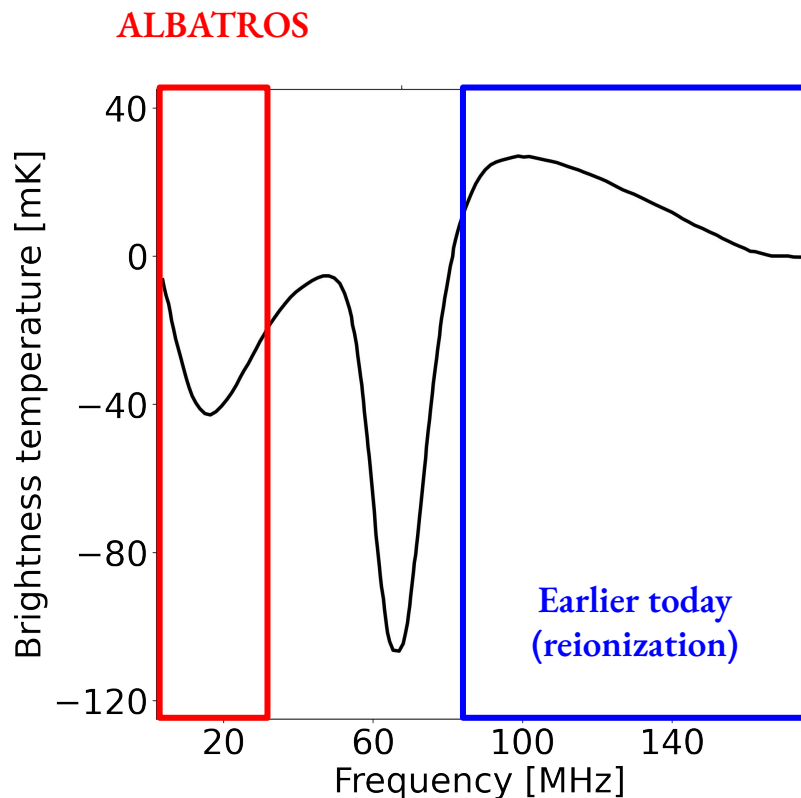
PI: Cynthia Chiang

ALBATROS Overview

- The **A**rray of **L**ong **B**aseline **A**ntennas for **T**aking **R**adio **O**bservations from the **S**ub-antarctic/**S**eventy-ninth parallel
- Goal: map the sky below 30 MHz
- Remote locations to minimize RFI
- Autonomous antenna stations with ~10 km baselines

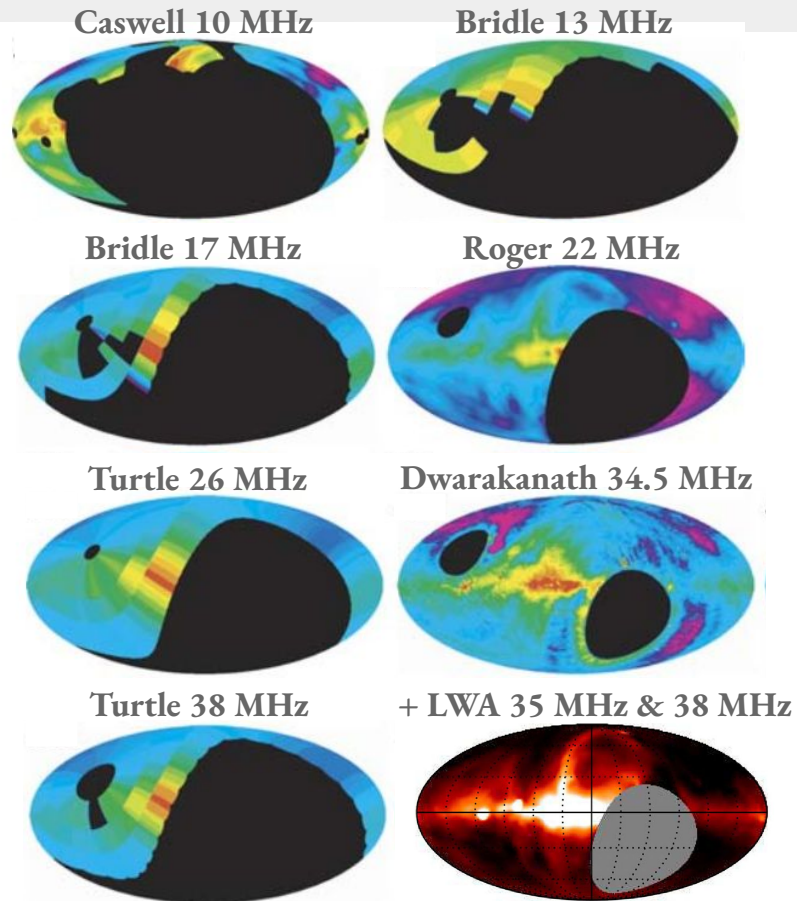
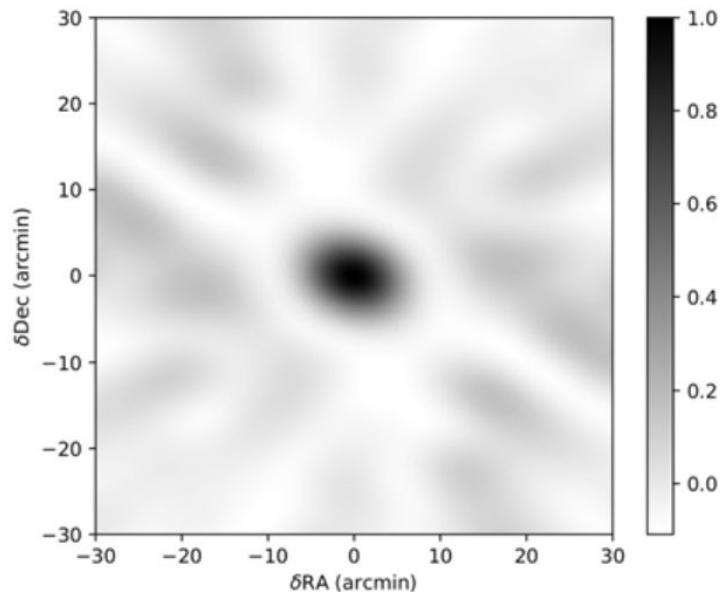


ALBATROS Overview

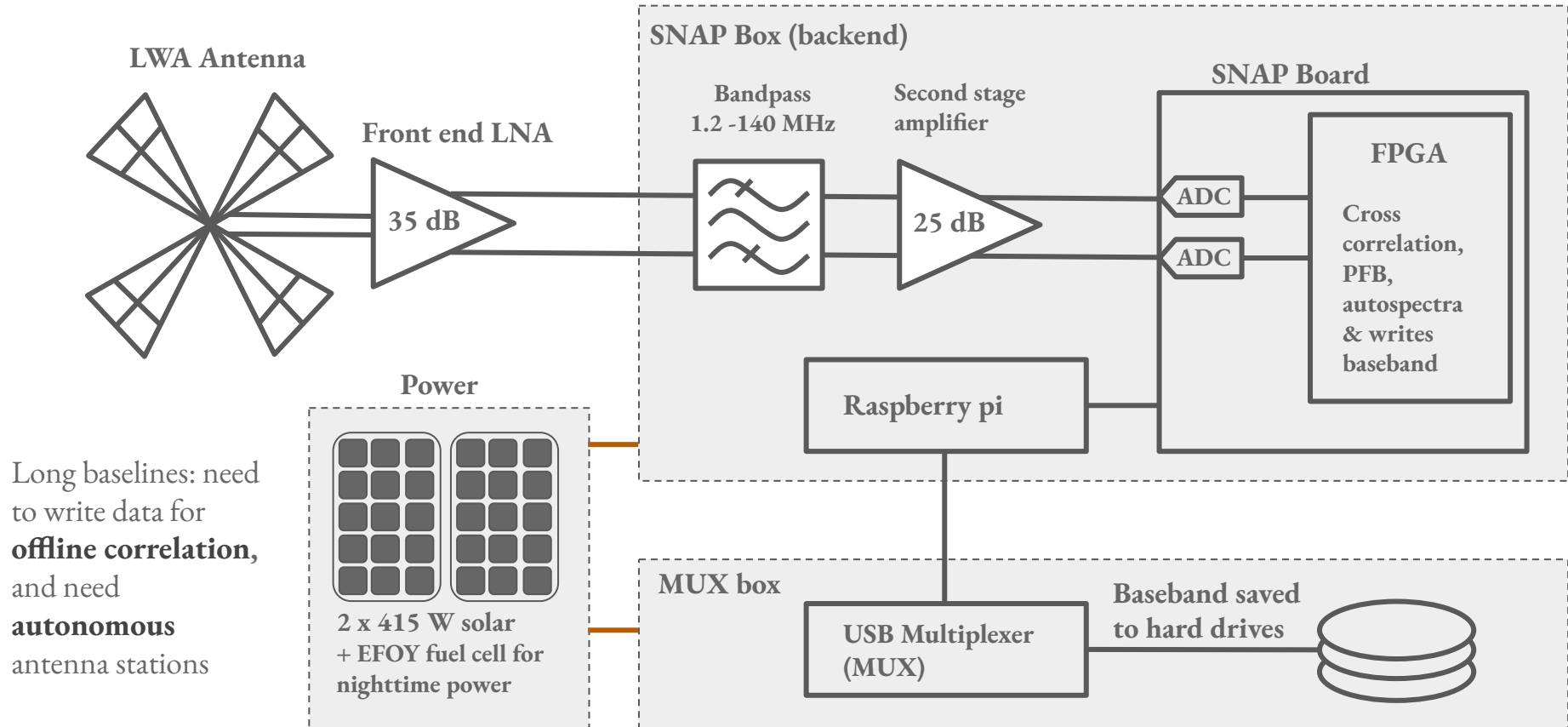


ALBATROS Overview

ALBATROS Synthesized beam at 5 MHz



Simplified ALBATROS block diagram

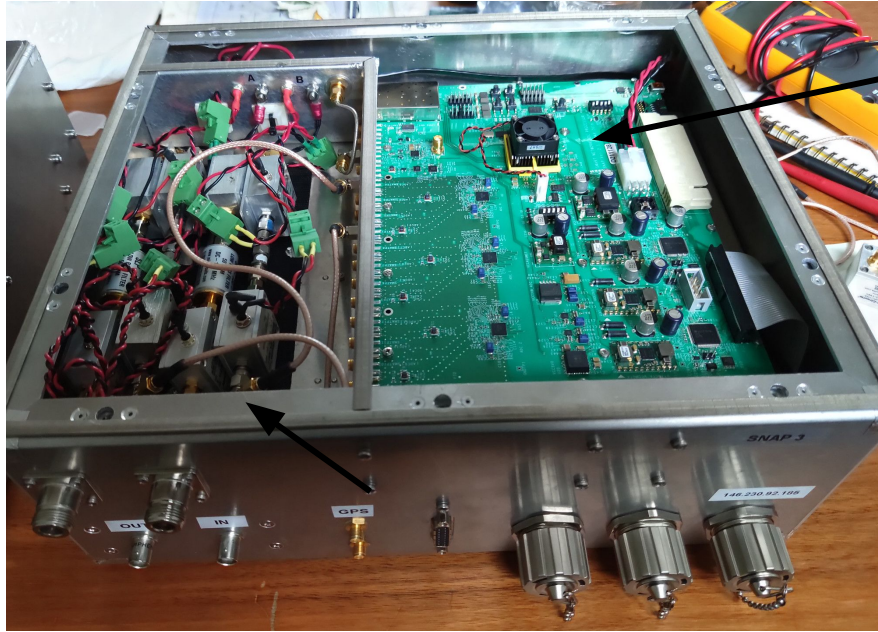


Another requirement: must be low profile



Maxed out Twin Otter load
~20k CAD per Otter flight

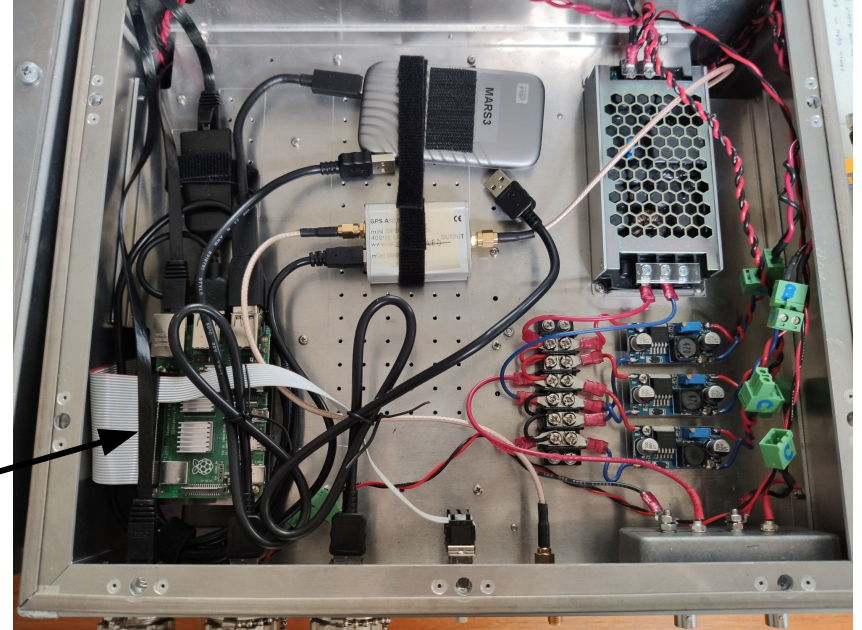
Back-end and readout electronics



SNAP board:
0-125 MHz
250 msamples/s
2048 frequency channels (61 kHz)

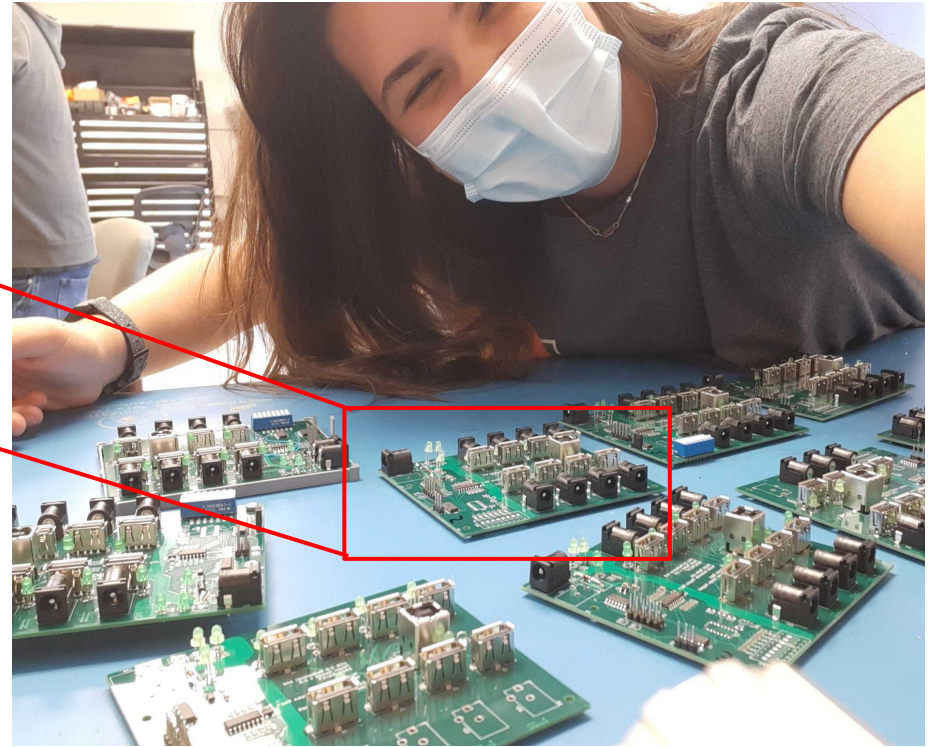
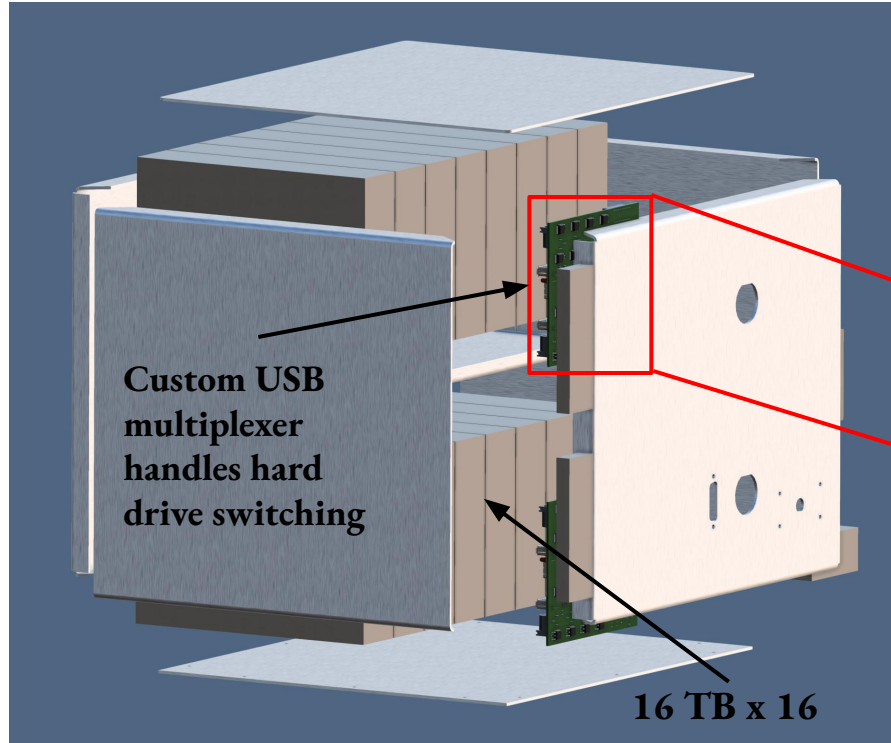
Total system power draw ~ 45 W
Can easily fit in a backpack

Raspberry Pi



Data storage

- Store 1 bit of baseband data for ~1 year of autonomous operation



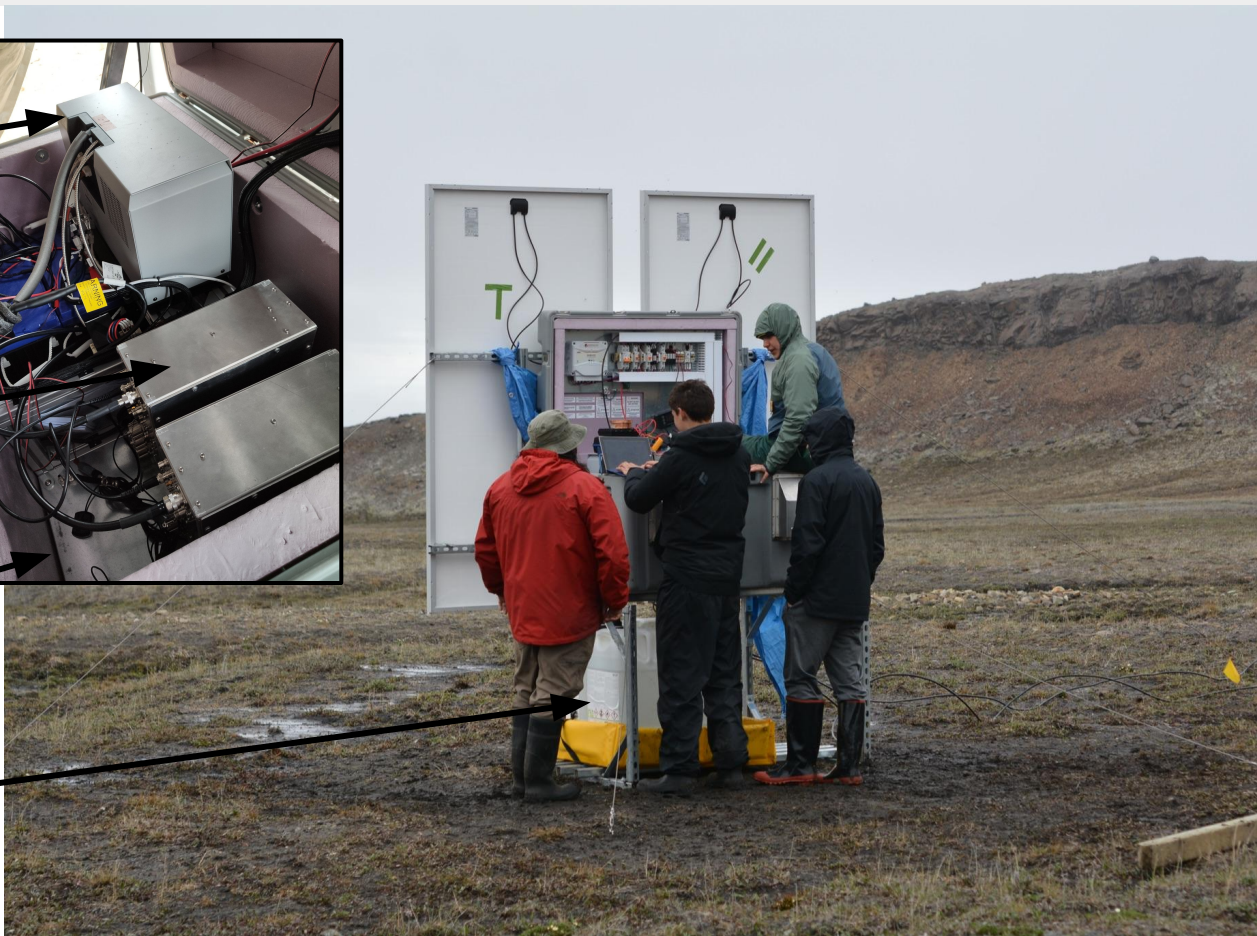
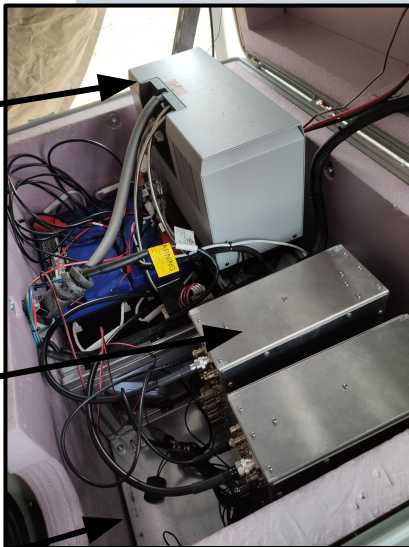
Power autonomy

Off the shelf hybrid
solar and methanol
generator (EFOY Pro
Energy box)

Back-end electronics box

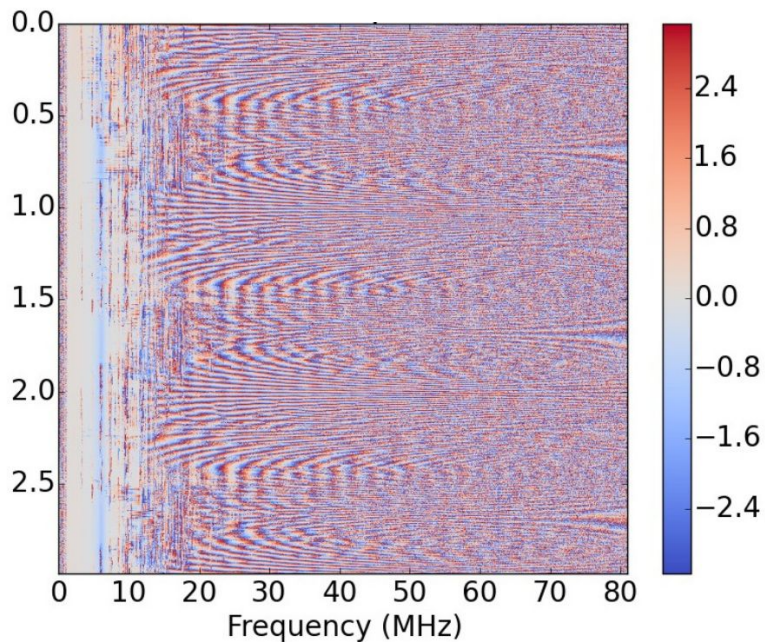
Hard drive box

Methanol tanks: 60L x 4



Front end amplifier and antenna response

- Currently using the long wavelength array (LWA) antenna and front end electronics: not optimized for these lowest frequencies.

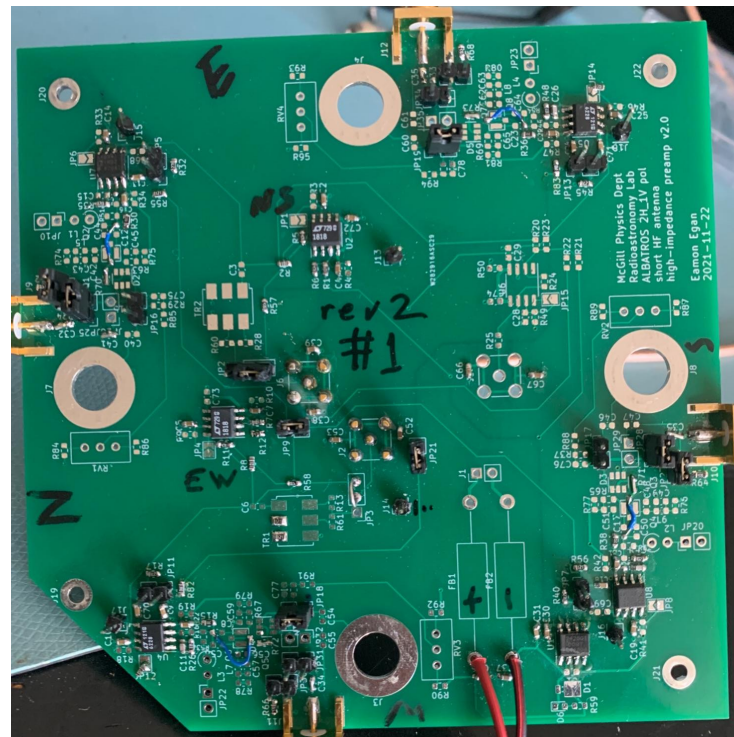
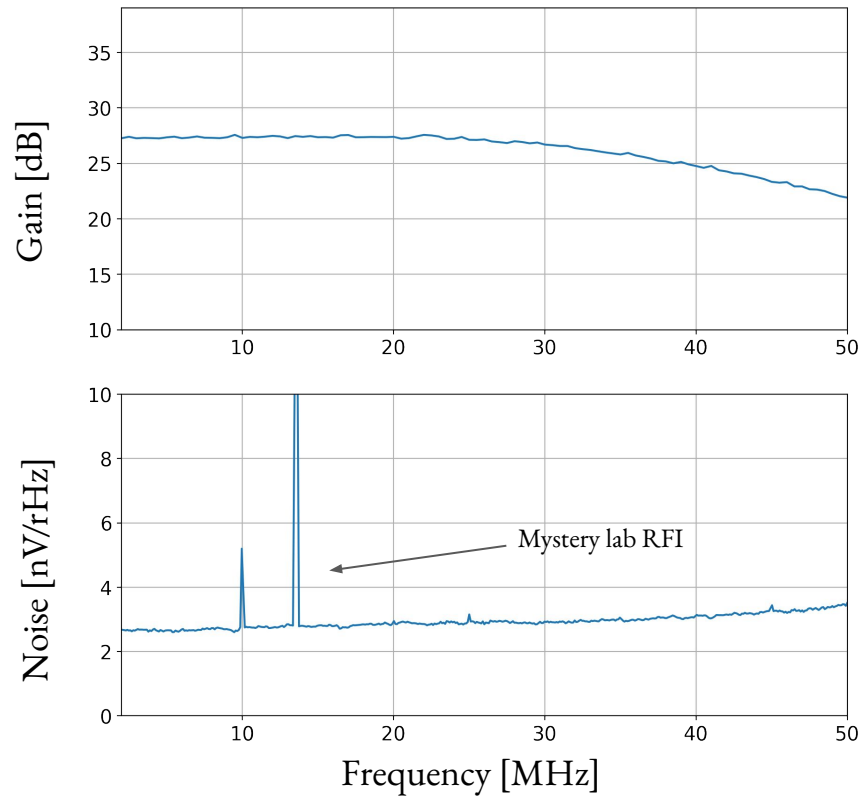


Cross spectra of 2-antenna
pathfinder at Marion island (LWA)



Front-end electronics (FEE) development

■ Custom high-impedance low-noise instrumentation amplifier



Team currently on site at Uapishka!



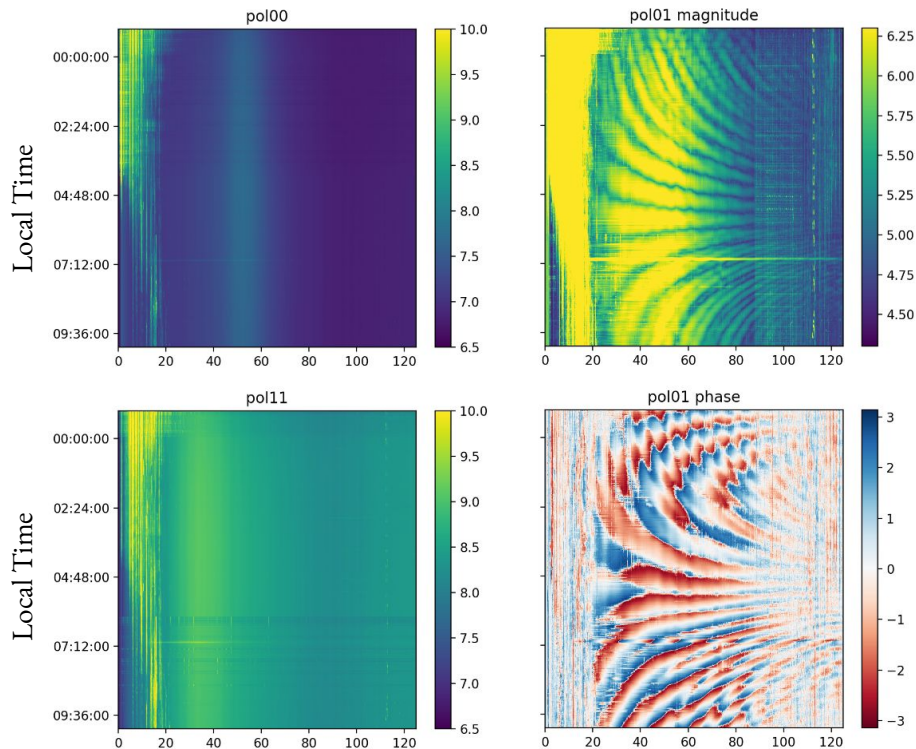
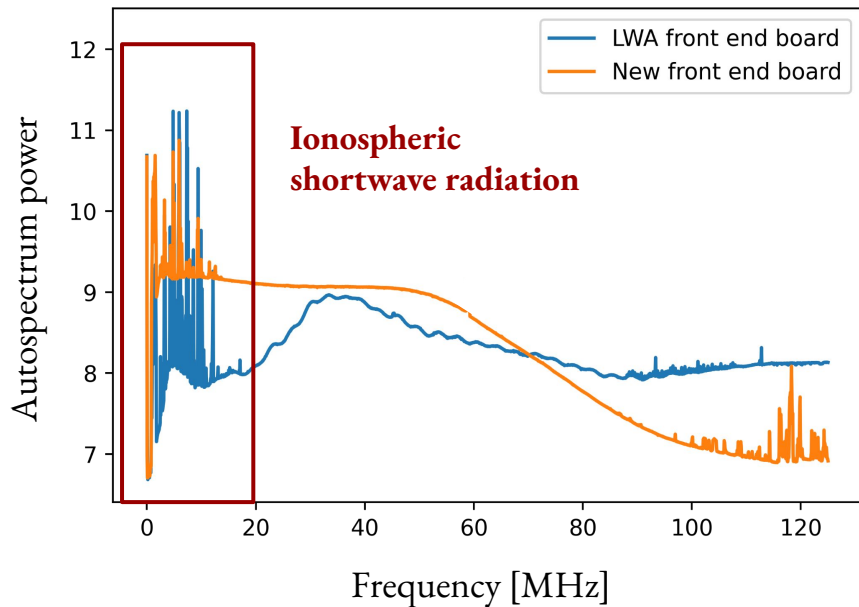
Jack Orlowski-Scherer
(formerly of ACT/SO)

Precision snow shovel
for data extraction

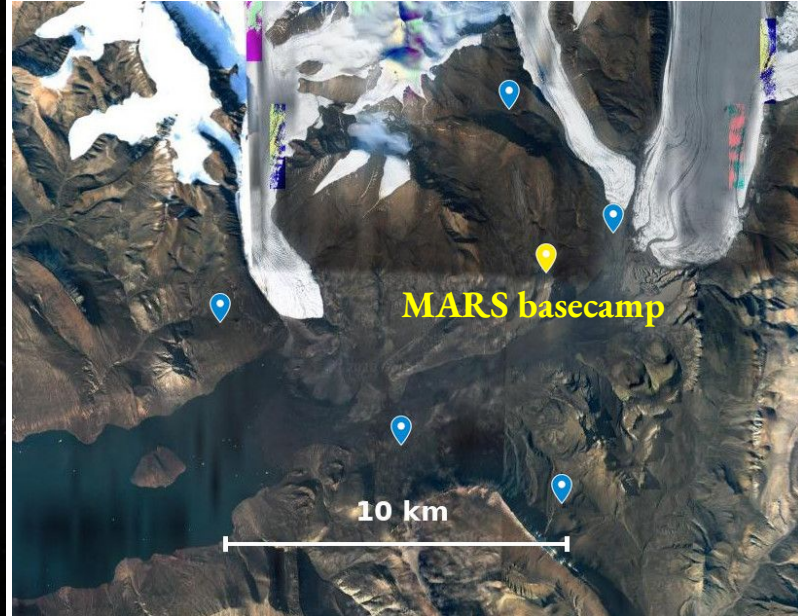
FEE is alive in here (not temperature controlled)



FEE proof of life: interferometric fringes



The McGill Arctic Research Station (MARS)



MARS basecamp







ALBATROS

Treacherous daily commute to work

ALBATROS



Success for the 2022 field season! First Arctic baseline



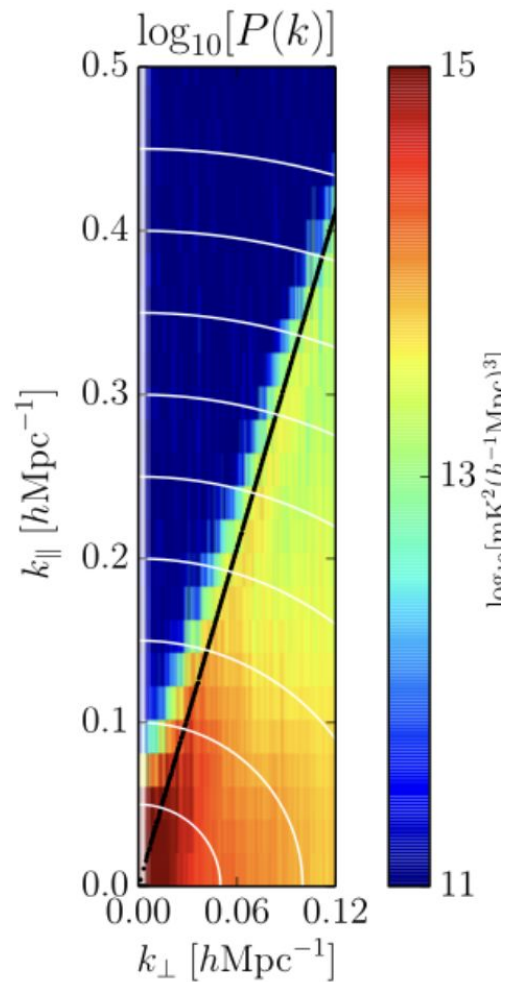
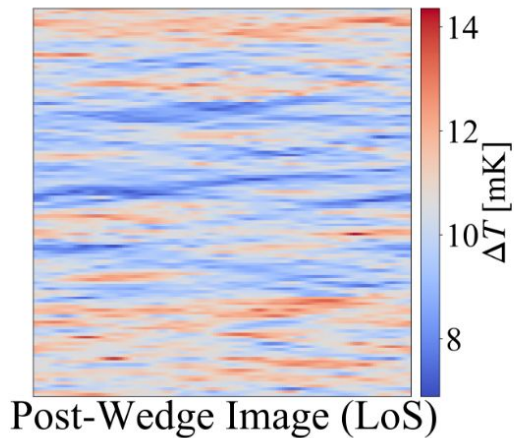
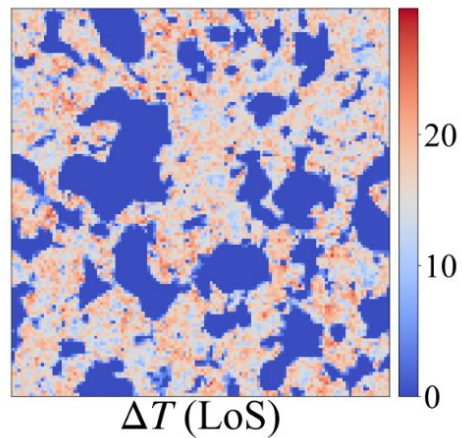
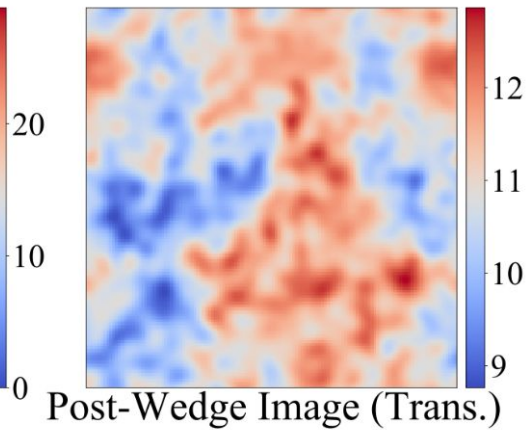
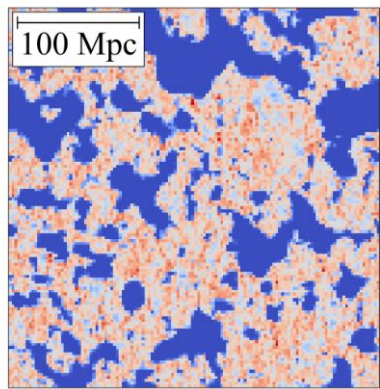
Success for the 2022 field season! First Arctic baseline

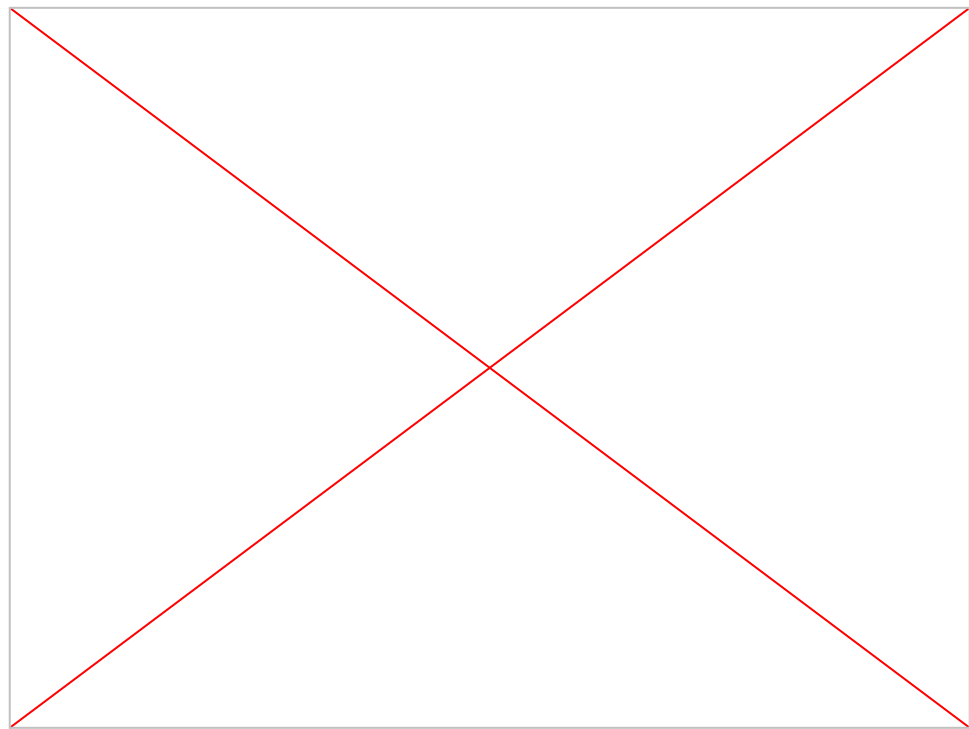


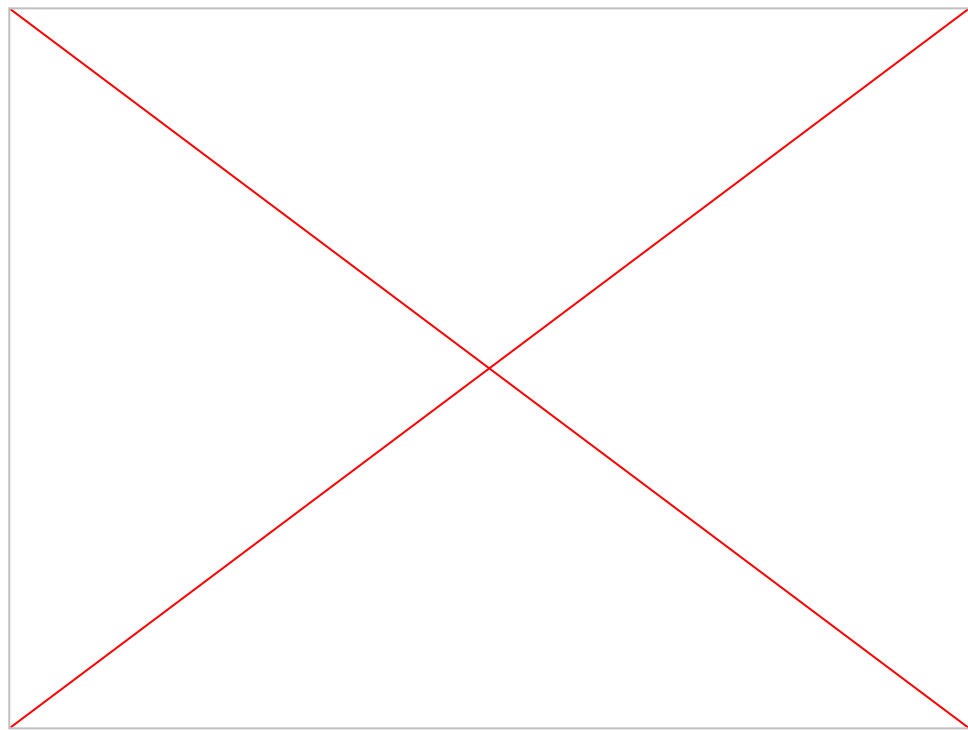
Next steps for ALBATROS:

- 3 new antenna stations in the Arctic for 2023.
- Continued antenna and FEE development.
- Keep working on satellite timing for offline cross-correlation.
- Starlink to phone home?
- Drone beam mapping.

BACKUP SLIDES







Simulating covariances: global 21cm signal

$$(\mathbf{C}_{\alpha\beta}^{21})^{-1} \approx \mathbf{F}_{\alpha\beta}^{21} = \sum_i \frac{\partial T_{21}(z_i)}{\partial x_{HI}(z_\alpha)} \mathbf{\Pi}_{\alpha\beta} \frac{\partial T_{21}(z_i)}{\partial x_{HI}(z_\beta)}$$

Approximated as analytic

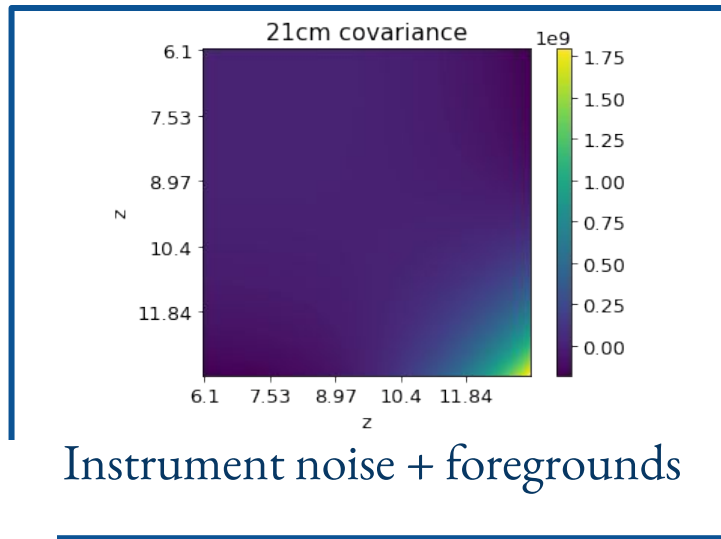
$$\delta T_b \approx 27 x_{HI} \left(\frac{1+z}{10} \right)^{1/2} \text{ mK}$$

$$(\mathbf{\Pi}_{\text{fg}})_{\nu\nu'} = A^2 \left(\frac{\nu\nu'}{\nu_*^2} \right)^{-\alpha + \frac{1}{2} \Delta \alpha^2 \ln(\nu\nu'/\nu_*^2)} - m(\nu) m(\nu'), \quad (6)$$

with¹

$$m(\nu) = A \left(\frac{\nu}{\nu_*} \right)^{-\alpha + \frac{1}{2} \Delta \alpha^2 \ln(\nu/\nu_*)}, \quad (7)$$

$$\sigma_i^2 = \frac{T_{\text{sky}}^2(\nu_i)}{b t_{\text{int}}},$$



Simulating covariances: kSZ

$$(\mathbf{C}_{\alpha\beta}^{kSZ})^{-1} \approx \mathbf{F}_{\alpha\beta}^{kSZ} = \sum_i \left[\frac{\partial C_\ell(\ell_i)}{\partial x_{HI}(z_\alpha)} \right] \mathbf{\Pi}_{\alpha\beta} \left[\frac{\partial C_\ell(\ell_i)}{\partial x_{HI}(z_\beta)} \right]$$

adeliegorce / tools4reionisation

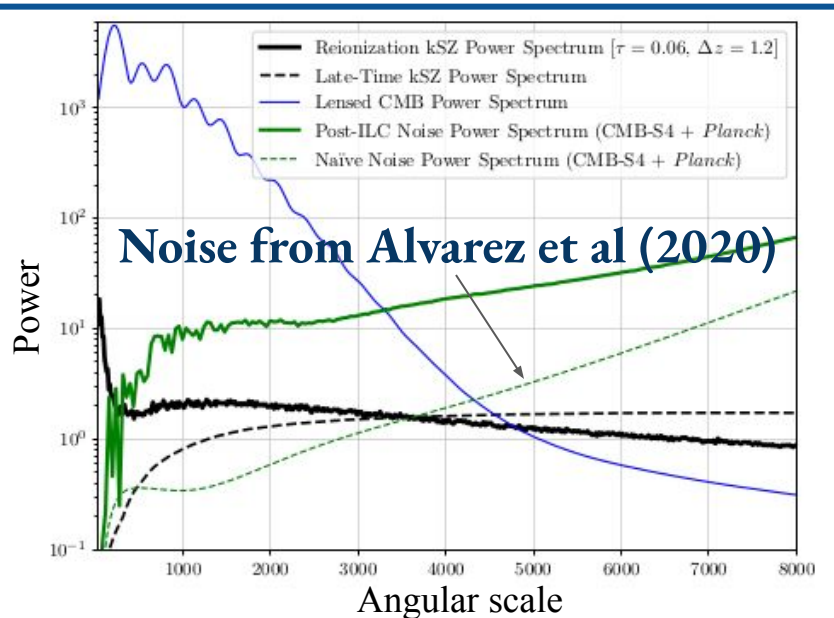
<> Code Issues Pull requests Actions Projects Wiki S

master 1 branch 0 tags

adelie gorce Modified tau computation

comprehensive_scenario	Merge b
ksz_power	Modified
star_formation_history	Correcte
LICENSE	Initial co
README.md	Code to

Numerical
derivatives of
kSZ power
spectrum



$$\mathbf{F}_{\text{kSZ}} \mathbf{v} = \lambda \mathbf{F}_{21} \mathbf{v}, \quad (15)$$

where \mathbf{F}_{kSZ} and \mathbf{F}_{21} are the Fisher matrices of the kSZ and 21cm global signal, respectively. Performing a Cholesky decomposition on the 21 cm covariance $\mathbf{C}_{21} = \mathbf{F}_{21}^{-1}$ allows us to write

$$\mathbf{F}_{21} = \mathbf{C}_{21}^{-1} = \mathbf{L}_{21}^{-T} \mathbf{L}_{21}^{-1}, \quad (16)$$

where \mathbf{L}_{21} is a lower triangular matrix. Equation 15 then becomes

$$\mathbf{L}_{21}^T \mathbf{F}_{\text{kSZ}} \mathbf{L}_{21} \mathbf{L}_{21}^{-1} \mathbf{v} = \lambda \mathbf{L}_{21}^{-1} \mathbf{v}, \quad (17)$$

which reduces to an eigenvalue problem

$$\mathbf{G} \mathbf{w} = \lambda \mathbf{w}, \quad (18)$$

with $\mathbf{G} \equiv \mathbf{L}_{21}^T \mathbf{F}_{\text{kSZ}} \mathbf{L}_{21}$ and $\mathbf{w} \equiv \mathbf{L}_{21}^{-1} \mathbf{v}$. With these definitions, we define the KL transformation matrix as

$$\mathbf{R} \equiv \mathbf{L}_{21} \mathbf{\Psi}, \quad (19)$$

where the columns of $\mathbf{\Psi}$ are the eigenvectors \mathbf{w} satisfying Equation 18. If we have a measurement of the ionization history $\mathbf{x} = (x_i(z_1), x_i(z_2), \dots, x_i(z_n))$, its representation \mathbf{y} in the KL basis is given by

$$\mathbf{y} = \mathbf{R}^{-1} \mathbf{x}, \quad (20)$$

and the inverse relation is

$$\mathbf{x} = \mathbf{R} \mathbf{y}. \quad (21)$$

In the KL basis, the information content (as expressed by the Fisher information matrices) is diagonal for both global 21 cm and kSZ measurements. Transforming their respective Fisher matrices via appropriate Jacobian factors, we obtain

$$\bar{\mathbf{F}}_{21} = \mathbf{\Psi}^T \mathbf{L}_{21}^T \mathbf{F}_{21} \mathbf{L}_{21} \mathbf{\Psi} = \mathbf{\Psi}^T \mathbf{\Psi} = \mathbf{I}, \quad (22)$$

for the 21 cm Fisher matrix in the KL basis and

$$\bar{\mathbf{F}}_{\text{kSZ}} = \mathbf{\Psi}^T \mathbf{L}_{21}^T \mathbf{F}_{\text{kSZ}} \mathbf{L}_{21} \mathbf{\Psi} = \mathbf{\Psi}^T \mathbf{G} \mathbf{\Psi} = \mathbf{\Lambda} \quad (23)$$

$$(\delta \mathbf{y}_{\text{kSZ}})_\alpha = \sum_\gamma (\bar{\mathbf{F}}_{\text{kSZ}}^{-1} \mathbf{R}^T)_{\alpha\gamma} \frac{\partial \mathbf{D}^T}{\partial x_i(z_\beta)} \mathbf{\Pi}_{\text{kSZ}}^{-1} \delta \mathbf{D}. \quad (43)$$

To simulate the CMB primary contaminating our kSZ measurement, we take $\delta \mathbf{D}$ to be a scaled primary CMB power spectrum. We allow the residual primary CMB temperature at $\ell = 3000$, $\delta D_{\ell=3000}^{\text{CMB}}$, to range up to $0.3 \mu\text{K}^2$ and find that even for small primary CMB residuals, \mathbf{z} is perturbed well outside the error bars for the overlap modes. This is unsurprising due to the large dynamic range of the CMB power spectrum over the range of ℓ that we are considering. Although a CMB temperature of $1 \mu\text{K}^2$ at $\ell = 3000$ is of the same order as the kSZ signal at this ℓ , the CMB can be up to two orders of magnitude brighter on the lower end of our ℓ range.

$$\nu \equiv \frac{|\mathbf{s}^T \mathbf{\Sigma}^{-1} \mathbf{z}|}{\sqrt{\mathbf{s}^T \mathbf{\Sigma}^{-1} \mathbf{s}}}.$$

